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**Reg. No. :**

## **Question Paper Code: U2M08**

# B.E./B.Tech. DEGREE EXAMINATION, NOV 2022

## Second Semester

Computer Science and Business Systems

21UMA208- LINEAR ALGEBRA AND NUMERICAL METHODS

(Regulations 2021)

Duration: Three hours

**Maximum: 100 Marks**

## Answer ALL Questions

### PART A - (10 x 1 = 10 Marks)

1. If the Eigen value of a matrix A are 1,2,3 then the Eigen value of  $A^T$  CO1-App  
 (a) 2,4,6 (b) 1,4,9 (c) 2,8,18 (d) 1,2,3

2. If the Eigen value of the matrix  $A = \begin{pmatrix} 1 & 1 \\ 3 & -1 \end{pmatrix}$  are 2,-2 then the Eigen value of  $A^{-1}$  are \_\_\_\_\_ CO1-App  
 (a)  $\frac{1}{2}, -\frac{1}{2}$  (b) 2,-2 (c) 1,-1 (d) 1,3

3. Solve the linear system  $5x+4y=15, 3x+7y=12$  gauss –Jordan method CO2-App  
 (a)  $\frac{57}{23}, \frac{15}{23}$  (b)  $\frac{15}{23}, \frac{15}{23}$  (c)  $\frac{5}{23}, \frac{15}{23}$  (d)  $\frac{57}{23}, \frac{5}{23}$

4. By Gauss elimination method, solve  $x + y = 2, 2x + 3y = 5$  CO2-App  
 (a) 1,2 (b) 1,1 (c) 1,0 (d) 0,1

5. Gauss Seidel method iteration converges if the coefficient matrix is dominant CO3- U  
 (a) Squarely (b) Logically (c) Diagonally (d) Symmetrically

6. The order of convergence of Newton's method is \_\_\_\_\_ CO3- U  
 (a) 1 (b) 2 (c) 3 (d) 0

7. In a vector space  $V$ , for every  $x, y \in V$  then property  $x+y=y+x$  is known as \_\_\_\_\_ CO6-R  
 (a) Commutative      (b) Associative      (c) identity      (d) Inverse
8. The  $\dim(\mathbb{R}^3)$  is \_\_\_\_\_ CO6-U  
 (a) 1      (b) 2      (c) 3      (d) 0
9.  $\langle x, x \rangle = 0$  if and only if then find  $x$  \_\_\_\_\_ CO6-U  
 (a)  $x=1$       (b)  $x \neq 1$       (c)  $x=0$       (d)  $x \neq 0$
10. The norm of  $(3, -4, 0)$  is \_\_\_\_\_ CO6-R  
 (a) 3      (b) -4      (c) 0      (d) 5

PART – B (5 x 2= 10 Marks)

11. If the Eigen value of the matrix  $A = \begin{pmatrix} 1 & 1 \\ 3 & -1 \end{pmatrix}$  are 2,-2 then find the Eigen value of  $A^{-1}$  CO1-App
12. Apply Gauss –Jordan method solve the linear system  $x + y = 2; 2x + 3y = 5$ . CO2-App
13. Explain Newton's backward interpolation formula CO6-R
14. Find the matrix of  $T : V_2(\mathbb{R}) \rightarrow V_3(\mathbb{R})$  given by  $T(a, b) = (a + 3b, 0, 2a - 4b)$  for the standard Basis of  $V_2(\mathbb{R})$  CO4-App
15. Explain rank-nullity theorem CO6-U

PART – C (5 x 16= 80Marks)

16. (a) Using Cayley Hamilton theorem find  $A^4$  and  $A^{-1}$  when  $A =$  CO1-App (16)

$$\begin{pmatrix} 7 & 2 & -2 \\ -6 & -1 & 2 \\ 6 & 2 & -1 \end{pmatrix}.$$

Or

- (b) Apply the orthogonal transformation reduce the following quadratic forms into canonical form CO1- App (16)  
 $Q = 6x^2 + 3y^2 + 3z^2 - 4xy - 2yz + 4zx$ , find its rank, index, signature and nature

17. (a) (i) Apply Gauss elimination method to solve  $2x+y+4z=12$ ,  $8x-3y+2z=1$ ,  $4x+11y-z=33$  CO2-App (8)

(ii) Apply Gauss Jordan method to solve  $10x+y+z=12$ , CO2-App (8)  
 $2x+10y+z=13$ ,  $x+y+5z=7$

Or

(b) Solve by using LU decomposition method CO2 -App (16)  
 $2x+5y+2z=18$ ;  $x+2y+3z=14$ ;  $3x+y+5z=20$

18. (a) (i) Using Lagrange's interpolation formula calculate the profit in CO3-App (8)  
the year 2000 from the following data :

year	1997	1999	2001	2002
Profit ( Rs.in lakhs)	43	65	159	248

(ii) Apply Newton Raphson Method Calculate a root of CO3-App (8)  
 $x \log_{10} x - 1.2 = 0$  correct to 3 decimals.

Or

(b) Calculate the dominant Eigen value and corresponding Eigen vector of A. if CO3-App (16)

$$A = \begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}.$$

19. (a) Construct the linear transformation  $T : V_3(R) \rightarrow V_3(R)$  determine CO4-App (16)

by the matrix  $\begin{pmatrix} 1 & 2 & 1 \\ 0 & 1 & 1 \\ -1 & 3 & 4 \end{pmatrix}$  with respect the standard basis of  $V_3(R)$

Or

(b) Let  $T : R^2 \rightarrow R^2$  by  $T(a_1 + a_2, a_1)$ , Calculate nullity(T), rank(T), Is CO4-App (16)  
T one-to-one and Is T is onto?

20. (a) (i) Show that the following function defines an inner product on  $V_2(R)$  where  $x = (x_1, x_2)$  and  $y = (y_1, y_2)$  and CO5-App (8)

$$\langle x, y \rangle = 6x_1y_1 + 7x_2y_2$$

(ii) If  $x = (2, 1+i, i)$  and  $y = (2-i, 2, 1+2i)$  then verify Schwarz's inequality. CO5-App (8)

Or

(b) Show that  $V_2(R)$  is an inner product space with inner product CO5-App (16)

defined by  $\langle x, y \rangle = x_1y_1 + x_2y_1 + x_1y_2 + 4x_2y_2$  where

$$x = (x_1, x_2) \text{ and } y = (y_1, y_2)$$