

A

Reg. No. :

--	--	--	--	--	--	--	--	--	--

**Question Paper Code: 94022**

B.E./B.Tech. DEGREE EXAMINATION, NOV 2022

Fourth Semester

Electronics and Communication Engineering

19UMA422 - Probability and Statistics

(Regulations 2019)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

- The  $r^{\text{th}}$  moment about origin is CO6-U  
(a)  $\mu(X)$                       (b)  $\mu(X^2)$                       (c)  $\mu(X')$                       (d) None of the above
- The limiting form of a Binomial distribution is CO6-U  
(a) Exponential                      (b) Poisson                      (c) Normal                      (d) None of the above
- Large sample size is \_\_\_\_\_ CO6-U  
(a) 30                      (b)  $>30$                       (c)  $<30$                       (d) none of the above
- The degrees of freedom for the sample size  $n=25$  in t test is \_\_\_\_\_. CO6-U  
(a) 20                      (b) 22                      (c) 24                      (d) 26
- Choose the correction factor \_\_\_\_\_ CO6-U  
(a)  $T^2N$                       (b)  $T/N$                       (c)  $T^2/N$                       (d)  $TN$
- SSE for Latin square design is CO6-U  
(a)  $TSS-SSC-SSR$                       (b)  $TSS-SSC$                       (c) 0                      (d)  $TSS-SSC-SSR-SSK$
- If the Random Process  $\{X(t)\}$  with mean  $\mu$  has Auto correlation function CO4-App  
 $R(\tau) = 16 + 9e^{-|\tau|}$  Then the Variance of the process is  
(a) 16                      (b) 25                      (c) 6                      (d) 9
- Autocorrelation function is maximum at  $\tau =$  CO6-U  
(a) 0                      (b) 1                      (c) -1                      (d)  $\infty$

9. The system is said to be stable if CO6-U
- (a)  $\int_{-\infty}^{\infty} h(t) dt < \infty$       (b)  $\int_{-\infty}^{\infty} h(t) dt > \infty$       (c)  $\int_{-\infty}^{\infty} h(t) dt > 0$       (d) None of the above

10. The average power of the auto correlation function is  $R_{xx}(\tau) = 3e^{-3|\tau|}$  CO6-U
- (a) 3      (b) 6      (c) 2      (d) 0

PART – B (5 x 2= 10Marks)

11. The mean and standard deviation of the binomial distribution 20 and 4 respectively, Calculate the value of the parameter ‘n’. CO1-App
12. A sample of size 10 has mean 58, standard deviation 18.4 and population mean 50, Compute the calculated value of ‘t’ distribution. CO2-App
13. What are the basic principles in the design of experiment? CO6-U
14. State any two properties of an auto correlation function CO6-U
15. If  $\mu_x = 0$  then compute the value of  $\mu_y$  CO5-App

PART – C (5 x 16= 80Marks)

16. (a) (i) Obtain the Correlation coefficient for the following heights (in inches) of fathers X and their sons Y. CO1-App (8)

X	65	66	67	67	68	69	70	72
Y	67	68	65	68	72	72	69	71

- (ii) The number of monthly breakdowns of a computer is a R.V. having a Poisson distribution with mean equal to 1.8. Find the Probability that his computer will function for a month (a) Without a breakdown (b) With only one breakdown (c) With at least one breakdown CO1-App (8)

Or

- (b) (i) State and Prove the memory less property for an Exponential distribution CO1- App (8)
- (ii) In a large consignment of electric bulbs 10 % are defective. A random sample 20 bulbs are taken for inspection. Find the probability that (a) all are good bulbs (b) exactly three defective bulbs. CO1- App (8)

17. (a) Two researchers A and B adopted different techniques while rating the student's level. Identify the Sampling distribution; Can you say that the techniques adopted by them are significant? CO2-App (16)

Researchers	Below Average	Average	Above Average	Genius	Total
A	40	33	25	2	100
B	86	60	44	10	200
Total	126	93	69	12	300

Or

- (b) Two independent samples of sizes 9 and 7 from a normal population had the following values of the variables. CO2 -Ana (16)

Sample I	18	13	12	15	12	14	16	14	15
Sample II	16	19	13	16	18	13	15		

Identify the sampling distribution, Do the estimates of the population variance differ significantly.

18. (a) A completely randomized design experiment with 10 plots and 3 treatments gave the following results: CO3-Ana (16)

Plot No	1	2	3	4	5	6	7	8	9	10
Treatment	A	B	C	A	C	C	A	B	A	B
Yield	5	4	3	7	5	1	3	4	1	7

Or

- (b) The following is a Latin square of a design, when four varieties of seeds are being tested, Analyze the given data Set up the analysis of variance table and State your conclusion. CO3-Ana (16)

A 105	B 95	C 125	D 115
C 115	D 125	A 105	B 105
D 115	C 95	B 105	A 115
B 95	A 135	D 95	C 115

19. (a) (i) If the auto correlation function of the random binary transmission CO4-App (8)

is given by 
$$R_{XX}(\tau) = \begin{cases} 1 - |\tau| & ; |\tau| \leq 1 \\ 0 & ; |\tau| \geq 1 \end{cases}$$
 Compute the Power

spectral density function.

- (ii) Using the properties of auto correlation function, compute the CO4-App (8)

Mean , Mean Square value and Variance of  $R_{xx}(\tau) = \frac{25\tau^2 + 36}{4 + 6.25\tau^2}$

Or

- (b) If the power spectral density of a continuous process is CO4-App (16)

$$S_{xx}(\omega) = \frac{10\omega^2 + 35}{(\omega^2 + 4)(\omega^2 + 9)}$$
, Compute the auto correlation function and

the mean square value of the process

20. (a) A random process X (t) is the input to a linear system whose impulse CO5-App (16)

response is  $h(t) = 2e^{-t}$ ;  $t \geq 0$ . If the input auto correlation function of the process is  $R_{xx}(\tau) = e^{-2|\tau|}$  Compute the power spectral density and auto correlation function of the output process.

Or

- (b) If the input to a time invariant stable linear system is a wide sense CO5-App (16)

stationary process. Prove that the output will also be a wide sense stationary process