

Reg. No. :

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**Question Paper Code: 99702**

B.E./B.Tech. DEGREE EXAMINATION, APRIL 2025

Seventh Semester

Mechanical Engineering

19UME702 – FINITE ELEMENT ANALYSIS

(Regulation 2019)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

1. \_\_\_\_\_ is a Numerical method for solving problems of Engineering and mathematical physics. CO1- U  
(a) Finite Element Analysis (b) Finite Element Method  
(c) Both (a) & (b) (d) none of the above
2. The art of subdividing a structure into a convenient number of smaller element is known as..... CO1- U  
(a) Non – Structural Problems (b) Structural Problems  
(c) Discretization of structure (d) None of the above
3. \_\_\_\_\_ is a force acting at a particular point which causes displacement. CO1- U  
(a) Traction force (b) Body force (c) Point load (d) None of the above
4. Assemblage of bars is called \_\_\_\_\_ CO1- U  
(a) Truss (b) Beams (c) Spring (d) None of the above
5. Linear Strain Triangular Element has \_\_\_\_\_ number of nodes. CO1- U  
(a) 3 (b) 6 (c) 12 (d) 24
6. In plane strain analysis CO1- U  
(a)  $\rho_z = 0$  (b)  $\gamma_{xz} = 0$  (c)  $\gamma_{yz} = 0$  (d) All of the above
7. A motion which repeats itself after equal interval of time is called CO1- U  
(a) Cycle (b) Frequency (c) Counter flow (d) Damping

- 8 The causes of vibration is/are CO1- U  
 (a) Winds (b) Earthquakes (c) Elastic Nature (d) All of the above
- 9 In non-structural problems \_\_\_\_\_ at each nodal point is obtained CO1- U  
 (a) Displacement (b) Temperature (c) Stress (d) Strain
- 10 \_\_\_\_\_ is imaginary line that connects a series of points CO1- U  
 (a) Path Line (b) Stream Line (c) Inviscid Flow (d) None of the above

PART – B (5 x 2= 10Marks)

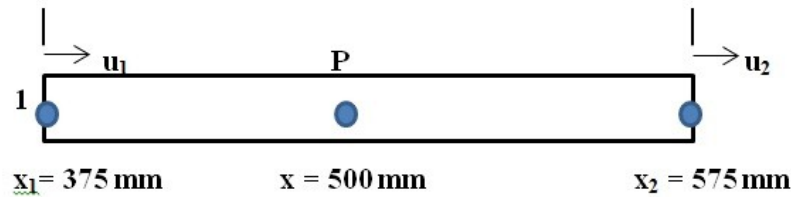
- 11 Explain the Aspect Ratio. CO1- U
- 12 Explain Degrees of freedom. CO1- U
- 13 Write down the stress-strain relationship matrix for plane strain condition. CO1- U
- 14 State difference between Direct and Iterative methods for solving system of equations. CO1- U
- 15 Write down the expression for stiffness matrix in 2D fluid mechanics. CO1- U

PART – C (5 x 16= 80 Marks)

- 16 (a) The following differential equation is available for a physical phenomenon. CO2- App (16)  

$$\frac{d^2y}{dx^2} + 50 = 0, 0 \leq x \leq 10$$
  
 and the trial function is  $y = a_{IX}(10-x)$  with boundary conditions as  
 $y(0) = 0$  and  $y(10) = 0$ . Find the value of the parameter  $a_I$  by the following methods.  
 (i) Point Collocation Method  
 (ii) Sub-domain Collocation Method  
 (iii) Least Squares Method  
 (iv) Galerkin's Method  
 Or
- (b) A beam AB of span L simply supported at ends and carrying a concentrated load W at the centre C. Analyze the deflection at mid-span by using Rayleigh Ritz method and compare with exact solution. CO4- Ana (16)
- 17 (a) Consider a bar as shown in figure. Cross-sectional area of the bar is  $750\text{mm}^2$  and Young's Modulus is  $2 \times 10^5 \text{ N/mm}^2$ . If  $u_1 = 0.5\text{mm}$  and  $u_2 = 0.625\text{mm}$ , calculate the following: CO2- App (16)  
 (i) Displacement at point, P  
 (ii) Strain,  $\epsilon$   
 (iii) Stress,  $\sigma$   
 (iv) Strain Energy, U

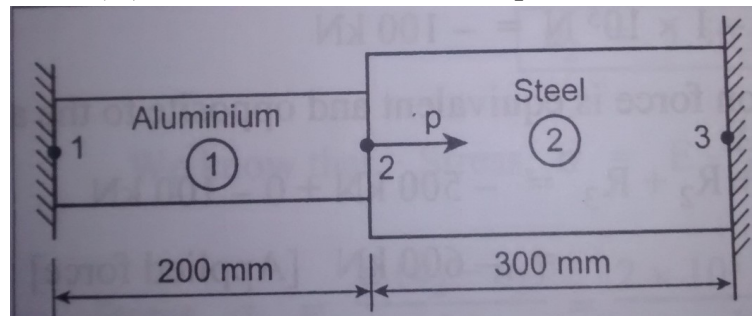
(v) Element Stiffness Matrix [K]



Or

- (b) An axial load of  $4 \times 10^5 \text{ N}$  is applied at  $30^\circ\text{C}$  to the rod as shown in the figure. The temperature is then raised to  $60^\circ\text{C}$ . Calculate the following:

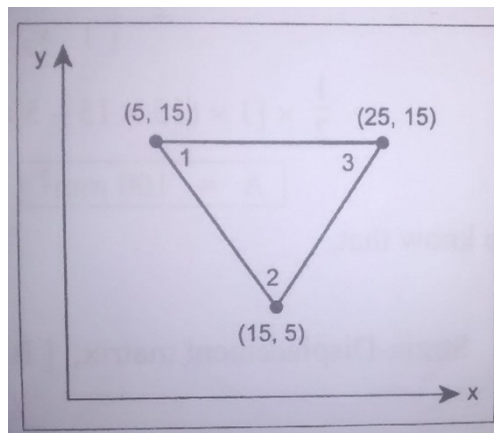
- Assemble the K and F matrices
- Nodal Displacements
- Stresses in each material
- Reactions at each nodal point



- 18 (a) For the plane strain element as shown in figure the nodal displacements are

$$\begin{aligned} u_1 &= 0.005 \text{ mm}; & v_1 &= 0.002 \text{ mm} \\ u_2 &= 0 \text{ mm}; & v_2 &= 0 \text{ mm} \\ u_3 &= 0.005 \text{ mm}; & v_3 &= 0 \text{ mm} \end{aligned}$$

Determine the element stresses  $\sigma_x$ ,  $\sigma_y$ ,  $\tau_{xy}$ ,  $\sigma_1$  and  $\sigma_2$  and the principal angle  $\Theta_p$ . Let  $E = 70 \text{ GPa}$ ,  $\nu = 0.3$  and use unit thickness. All coordinates are in mm



Or

CO2- App (16)

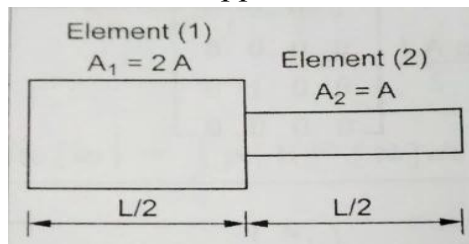
- (b) (i) Evaluate the integral  $\int_{-1}^1 \frac{\cos x}{1-x^2} dx$  by applying 3 point Gaussian Quadrature.

CO2- App (8+8)

(ii) Evaluate the integral  $\int_{-1}^1 (2 + x + x^2) dx$  and compare with exact solution.

Or

- 19 (a) Compare the natural frequencies of longitudinal vibration of the unconstrained stepped bar as shown in the figure. CO4- Ana (16)

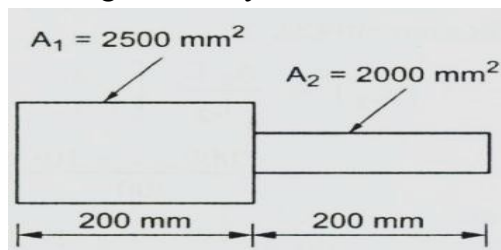


Or

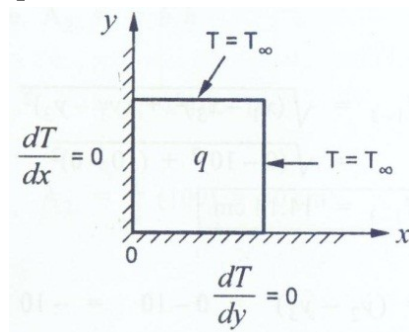
- (b) Compare the eigen values and frequencies for the stepped bar as shown in the figure. CO4- Ana (16)

Take, Young's modulus  $E = 2 \times 10^5 \text{ N/mm}^2$ ,

Unit weight Density  $= 0.8 \times 10^{-4} \text{ N/mm}^3$



- 20 (a) Evaluate the temperature distribution in a square region with uniform energy generation as shown in figure. Assume that there is no temperature variation in the z-direction. Take  $k=30 \text{ W/cm}^\circ\text{C}$ ,  $l=10 \text{ cm}$ ,  $T_\infty=50^\circ\text{C}$ ,  $q=100 \text{ W/cm}^3$ . CO6- Eva (16)



Or

- (b) A steel rod of diameter  $d = 2 \text{ cm}$ , Length  $L = 5 \text{ cm}$  and thermal conductivity  $k = 50 \text{ W/m}^\circ\text{C}$  is exposed at one end to a constant temperature of  $320^\circ\text{C}$ . The other end is in ambient air of temperature  $20^\circ\text{C}$  with a convection coefficient of  $h = 100 \text{ W/m}^2\text{C}$ . Evaluate the temperature at the midpoint of the rod. CO6- Eva (16)





