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Question Paper Code:R2M08

B.E./B.Tech. DEGREE EXAMINATION, APRIL / MAY 2025

Second Semester

Computer Science and Business systems

R21UMA208- LINEAR ALGEBRA AND NUMERICAL TECHNIQUES

(Regulations R2021)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

1. If 0,3,4 are the Eigen value of a matrix A then $|A| =$ _____ CO1- App
(a)12 (b)0 (c)3 (d) 4
2. If $A = \begin{pmatrix} a & 1 \\ 3 & b \end{pmatrix}$ has Eigen values of 2,-2 then a and b are _____ CO1- App
(a) 1,-1 (b) -1,-1 (c) 1,1 (d) 0,1
3. By Gauss elimination method, solve $x + y = 2$, $2x + 3y = 5$ CO2- App
(a)1,2 (b) 1,1 (c) 1,0 (d) 0,1
4. The principle of triangularisation method is _____ CO2-U
(a) A=LU (b) L=AU (c) U=LA (d) A=UI
5. Newton –Raphson method is used to find the root of the equation $x^2 - 2 = 0$ CO3- App
(a)-1 (b) $\sqrt{2}$ (c) $-\sqrt{2}$ (d) 0
6. The n^{th} divided difference of n^{th} degree polynomial is CO6- U
(a) constant (b) variable (c) equal (d) unequal
7. Any linear transformation $T : V \rightarrow W$ can be represented by a _____ CO6- U
(a) Line (b) Circle (c) square (d) matrix

8. A vector field in $\mathbb{R}^n$ is a function CO6- U
 (a) $F \text{ vector} \rightarrow 0$ (b) $F \text{ vector} \rightarrow \mathbb{R}^n: \mathbb{R}^n$ (c) $F \text{ vector} \rightarrow \mathbb{R}^n$ (d) $F \text{ vector}: \mathbb{R}^n \rightarrow \mathbb{R}^n$

9. In a vector space find $\|\alpha x\| = \underline{\hspace{2cm}}$ CO6- U
 (a) $|\alpha| + \|x\|$ (b) $|\alpha| - \|x\|$ (c) $|\alpha| \|x\|$ (d) $|\alpha| / \|x\|$

10. The norm of $(3, -4, 0)$ is CO5- App
 (a) -4 (b) 3 (c) 0 (d) 5

PART – B (5 x 2= 10 Marks)

11. Explain the Cayley Hamilton theorem and its uses CO6 -U
 12. Apply Gauss-Jordan method calculate the inverse of CO2-App

$$A = \begin{pmatrix} 1 & 3 \\ 2 & 7 \end{pmatrix}$$

13. Show that newton's Raphson formula to find $\sqrt{N}$ can be expressed in the CO3-App
 form $x_{n+1} = \frac{1}{2} \left[x_n + \frac{N}{x_n} \right]$.
 14. State any two properties of linear transformation CO6 -U
 15. Verify triangle inequality for the following data $\|x + y\| = 6, \|x\| =$ CO6- U
 $3 \text{ and } \|y\| = 4$

PART – C (5 x 16= 80 Marks)

16. (a) (i) Find all the eigenvalues and eigenvectors of the matrix CO1-App (8)

$$\begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{pmatrix}$$

- (ii) Using Cayley Hamilton theorem find A^{-1} when CO1-App (8)

$$A = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 2 & -3 \\ 2 & -1 & 3 \end{pmatrix}.$$

Or

- (b) Apply the orthogonal transformation reduce the following CO1-App (16)
 quadratic forms into canonical form

$Q = 6x^2 + 3y^2 + 3z^2 - 4xy - 2yz + 4zx$, find its rank, index, signature and nature

17. (a) (i) Apply Gauss elimination method to solve $5x-2y+3z=18, x+7y-3z=-22, 2x-y+6z=22$. CO2-App (8)
(ii) Solve the following system of equations by Gauss Jordan method $x+y+z=6, 3x+3y+4z=20, 2x+y+3z=13$ CO2-App (8)
Or
(b) Solve by using LU decomposition method CO2-App (16)
 $2x+5y+2z=18; x+2y+3z=14; 3x+y+5z=20$
18. (a) (i) Apply Newton Raphson Method Calculate a root of $x \log_{10} x - 1.2 = 0$ correct to 3 decimals. CO3- App (8)
(ii) Solve by using Gauss Seidal CO3-App (8)
 $3x-y+z=1, 3x+6y+2z=0, 3x+3y+7z=4$
Or
(b) (i) Using Lagrange's interpolation formula find $f(3)$ for the following data CO3- App (8)
- | | | | | |
|---|---|---|----|-----|
| X | 0 | 1 | 2 | 5 |
| Y | 2 | 3 | 12 | 147 |
- (ii) From the following data find y at $x=84$ CO3-App (8)
- | | | | | | | |
|---|-----|-----|-----|-----|-----|-----|
| X | 40 | 50 | 60 | 70 | 80 | 90 |
| Y | 184 | 204 | 226 | 250 | 276 | 304 |
19. (a) (i) Verify the vectors $(1,2,0), (2,3,0), (8,13,0)$ in R^3 is a basis of R^3 CO4- App (8)
(ii) Find the dimension of the subspace spanned by the vectors $(1,2,-3), (0,0,1), (-1,2,1)$ in $V_3(R)$ CO4- App (8)
Or
(b) (i) If $T: R^2 \rightarrow R^3$ be linear transformation defined by $T(a_1, a_2) = (a_1 - a_2, 0, 0)$ then find nullity (T), rank(T), Is T one-to-one? Is T onto? Also check the rank nullity theorem. CO4- App (8)
(ii) Find the matrix of the linear transformation $T: V_2(R) \rightarrow V_3(R)$ defined by $T(a, b) = (a-b, 2a, 3a+2b)$ for the standard basis of $V_2(R)$ CO4-App (8)
20. (a) Apply Gram-Schmidt process to construct an orthonormal basis for $V_3(R)$ with the standard inner product for the basis $\{v_1, v_2, v_3\}$ where $v_1 = (2, -1, 0), v_2 = (4, -1, 0)$ and $v_3 = (4, 0, -1)$ CO5- App (16)
Or

- (b) (i) Show that the following function defines an inner product on $V_2(\mathbb{R})$ where $x = (x_1, x_2)$ and $y = (y_1, y_2)$ and $\langle x, y \rangle = x_1 y_1 + x_2 y_1 + x_1 y_2 + 4x_2 y_2$ CO5- App (8)
- (ii) If $x = (2, 1 + i, i)$ and $y = (2 - i, 2, 1 + 2i)$ then verify triangle inequality. CO5- App (8)