Reg. No. :

Question Paper Code: U3028

B.E./B.Tech. DEGREE EXAMINATION, APRIL 2024

Third Semester

Computer Science and Design

21UMA328- DISCRETE MATHEMATICS

(Common to Aritificial Intelligence & Data Science Engineering)

(Regulations 2021)

Duration: Three hours

Maximum: 100 Marks

Answer All Questions

PART A - (10x 1 = 10 Marks)

- What is the value of x after this statement, assuming the initial value of x is 5? CO6-U If x equals to one then x=x+2 else x=0'.
 - (a) 1 (b) 3 (c) 0 (d) 2
- 2. The statement," Every comedian is funny" where C(x) is "x is a comedian" CO1- App and F (x) is "x is funny" and the domain consists of all people.

 $(a)\exists x(C(x) \land F(x)) \quad (b) \forall x(C(x) \land F(x)) \quad (c)\exists x(C(x) \rightarrow F(x)) \quad (d) \forall x(C(x) \rightarrow F(x))$

- 3. What is the base case for the inequality $7n > n^3$, where n = 3?CO2- App(a) 652 > 189(b)42 < 132(c)343 > 27(d) $42 \le 431$
- 4. The numbers between 1 and 520, including both, are divisible by 2 or 6 is CO2- App
 - (a) 349 (b)54 (c) 213 (d) 303
- 5. A group (M, *) is said to be abelian if ______CO6- U(a) (x + y) = (y + x)(b) (x * y) = (y * x)(c) (x + y) = x(d) (y * x) = (x + y)6. Intersection of subgroups is a ______.CO6- U(a) group(b) subgroup(c) semi group(d) cyclic group7. In a _____ the degree of each and every vertex is equal.CO6- U
 - (a) regular graph (b) point graph (c) star graph (d) Euler graph

A

8.	Every complete bipartite graph must not be				C	2 06- U	
	(a) p	planar graph	(b) line graph	(c) complete graph (d) subgraph		
9.	Which of the following Law of Boolean proofs the X. X=X? CO6-						
	(a) Identity Law (b) D			(b) Double Complement	Double Complement Law		
	(c) Complement Law			(d) Idempotent Law			
10.	Α_	A is a Boolean variable.				06- U	
	(a) Literal (b) String (c) Keyword (d) Ide				fier		
$PART - B (5 \times 2 = 10 Marks)$							
11.	Finc	d the value of the j	CO1- App				
12.	What is the generating function for generating series 1, 2, 3, 4, 5,?				CO2- App		
13.	Define cyclic group with an example.				CO6- U		
14.	Draw K ₅ complete graph.				CO6- U		
15.	State distributive lattice.				CO6- U		
PART – C (5 x 16= 80Marks)							
16.	(a)	(i) Find PDNF an	nd PCNF of $(P \land Q)$	$\vee (\neg P \land R).$	CO1 -App	(8)	
		(ii) Prove that (() is a tautology.	$p \lor q) \land \neg (\neg p \land (\neg q))$	$(\neg r))) \vee (\neg p \land \neg q) \vee (\neg p \land \neg r)$	CO1 -App	(8)	
	Or						
	(b)			onclusion from the premises using conditional proof.	CO1 -App	(8)	
		(ii) Show that the	at $\exists x P(x) \longrightarrow \forall x Q(x)$	$x) \Rightarrow \forall x \ (P(x) \longrightarrow Q(x)).$	CO1 -App	(8)	
17.	(a)	(i) Solve: a_{n+2} +	$-3a_{n+1}+2a_n=$	3^n , $a_0 = 0$, $a_1 = 1$	CO2 -App	(8)	
			ting functions Solv $a_{n-2} = 0, n \ge 2a_0$ Or		CO2 -App	(8)	

(b) (i) Prove that by using mathematical Induction $\frac{1}{1.2} + \frac{1}{2.3} + \text{CO2-App}$ (8) $\frac{1}{3.4} + \dots + \frac{1}{n(n+1)} = \frac{n}{(n+1)}$

(ii) Out of 100 students in a college, 38 play tennis, 57 play CO2 -App (8) cricket and 31 play hockey, 9 play cricket and hockey, 10 play hockey and tennis, 12 play tennis and cricket.
How many plays (1) All three games.

(2) Atleast two game.

(3) Hockeyor cricket but not tennis

(Assume that each student plays atleast one game.)

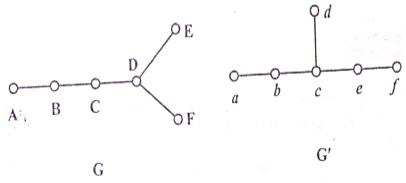
18. (a) (i) Show that $(Q^+,*)$ is an abelian group where * is defined as a*b CO3- App (8) = ab/2, $\forall a, b \in Q^+$. (ii) S.T by using an example "the union of two subgroup of a CO3- App (8)

group G need not be a subgroup".

Or

(b) (i) State and prove Lagrange's theorem. (ii) Prove that $(\boldsymbol{a}*\boldsymbol{b})^2 = \boldsymbol{a}^2*\boldsymbol{b}^2$ (ffy io abelian) CO3- App (8) CO3- App (8)

19. (a) (i) Verify that following are isomorphic graph are not CO4-App



(ii) Prove that a simple graph with n vertices must be connected if CO4-App (8) it has more than $\frac{(n-1)(n-2)}{2}$ edges. Or

(8)

(b) (i) Define Isomorphism between the two graphs. Are the simple CO4-App (8) graphs with the following adjacency matrices isomorphic?

г0 ן1 г0 0 1 0 1 0 0 1 and L_1 L1 (ii) Prove that a given connected graph is Eulerian if and only if CO4-App (8) all the vertices of G are of even degree.

- 20. (a) (i) State and prove the distributive inequalities of a Lattice. CO5- App (8) (ii) State and prove De Morgan's law for Boolean algebra. CO5- App (8) Or
 - (b) (i) Show that in a complemented distributive lattice, the De CO5-App (8) Morgan's laws hold good.

(ii) Show that in any Boolean algebra (a + b)(a' + c) = ac + CO5- App (8) a'b + bc = ac + a'b

$$\mathbf{a} \quad \mathbf{a} + \sqrt{\mathbf{a}^2 - \mathbf{y}^2}$$

$$\int \qquad \int \mathbf{x} \mathbf{y} \, \mathbf{d} \, \mathbf{x} \, \mathbf{d} \, \mathbf{y}$$

$$0 \quad \mathbf{a} - \sqrt{\mathbf{a}^2 - \mathbf{y}^2}$$