



8.  $\int_0^{\infty} 6e^{-x} x^5 dx$  CO4- App
- (a) 6                                      (b) 6!                                      (c) 7!                                      (d) 5!
9. The region of integration of the integral  $\int_0^1 \int_0^x f(x, y) dx dy$  is CO6- U
- (a) square                                      (b) rectangle                                      (c) triangle                                      (d) circle
10. The value of integral  $\int_1^2 \int_1^4 \frac{dx dy}{xy}$  CO5- App
- (a)  $\log 8$                                       (b)  $(\log 2)^2$                                       (c)  $\log 6$                                       (d) None of the above

PART – B (5 x 2= 10Marks)

11. Compute PDF for  $(P \vee Q)$  CO1- App
12. In how many ways can letters of the word “THUNAIEZHUTHU” be arranged CO2- App
13. For a Group  $G = \{1, -1, -i, i\}$  under multiplication ,Find order of all elements CO3- App
14. Compute  $y_{25}$  if  $y = \frac{1}{x}$  CO4- App
15. Solve  $\int_0^1 \int_0^2 x^2 y^2 dy dx$  CO5- App

PART – C (5 x 16= 80Marks)

16. (a) (i) Calculate PCNF and PDF for  $(P \wedge \neg Q) \vee (P \wedge R) \vee (Q \wedge R)$  CO1 -App (8)  
(ii) Using the rules of inference derive & using CP Rule. CO1 -App (8)  
 $P \rightarrow (Q \rightarrow V), \neg U \vee P, Q \Rightarrow U \rightarrow (V \wedge P)$
- Or
- (b) (i) Prove the following by Indirect Method. CO1 -App (8)  
 $P \rightarrow (Q \wedge R), (Q \vee S) \rightarrow U, P \vee S \Rightarrow U$
- (ii) Show that the premises “one student in this class knows how to write programs in JAVA”and “Every one who knows how to write programs in JAVA can get a high- paying job” imply the conclusion “some one in this class can get high paying job CO1 -App (8)

17. (a) (i) Using mathematical induction show that  $n^3 + (n+1)^3 + (n+2)^3$  is a multiple of 9. CO2 -App (8)
- (ii) Solve  $a_n - 4a_{n-1} + 4a_{n-2} = 2^n, a_0 = 1, a_1 = 1$ . CO2 -App (8)
- Or
- (b) (i) Calculate the number of positive integers not exceeding 1200 that are divisible by 2, 3, 5 or by 7. CO2 -App (8)
- (ii) Using generating functions Solve  $a_n = 3a_{n-1} + 5^n, a_0 = 4$ . CO2 -App (8)
18. (a) (i) Let G be a finite group of order 'n' and H be any subgroup of G. Then Show that the order of H divides the order of G. (i.e)  $O(H) / O(G)$  CO3- App (8)
- (ii) Show that  $(Q^+, *)$  is an abelian Group. Where \* defined as  $a*b = \frac{ab}{2}$  where  $a, b \in Q^+$  CO3- App (8)
- Or
- (b)  $S = Q \times Q$ , such that binary operation defined by  $(a, b) * (x, y) = (ax, ay + b)$  CO3- App (16)
- (i) Prove that  $(S, *)$  is a semi group
- (ii). Is it commutative and calculate the value of  $(2,4)*(1,5)$
- (iii) Find the identity Element
- (iv) Find the inverse of  $(2,3)*(8,6)$  and  $(0,2)*(3,5)$
19. (a) (i) If  $y = a \cos(\log x) + b \sin(\log x)$  Show that  $x^2 y_2 + xy_1 + y = 0$  CO4-App (8)
- (ii) Compute the value of a,b,c if  $\lim_{x \rightarrow 0} \frac{ae^x - be^{-x} - cx}{x - \sin x} = 4$  CO4-App (8)
- Or
- (b) (i) Compute  $\int_0^{\frac{\pi}{2}} \frac{dx}{1 + \sqrt{\tan x}}$  CO4-App (8)
- (ii) Evaluate  $\lim_{x \rightarrow 0} \frac{xe^x - \log(1+x)}{x^2}$  CO4-App (8)

20. (a) (i) Find the volume of the tetrahedron bounded by  $6x + 4y + z = 12$ ,  $x = 0$ ,  $y = 0$ ,  $z = 0$ . CO5- App (8)

(ii) Compute the area between the parabola  $y^2 = x$  and  $x^2 = y$  CO5- App (8)

Or

(b) (i) Evaluate  $\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} \frac{dx dy dz}{\sqrt{1-x^2-y^2-z^2}}$  CO5- App (8)

(ii) Change the order of integration and hence evaluate CO5- App (8)

$$\int_0^a \int_{a-\sqrt{a^2-y^2}}^{a+\sqrt{a^2-y^2}} xy dx dy$$