A		Reg. No. :					
Question Paper Code: U3027							
B.E./B.Tech. DEGREE EXAMINATION, APRIL 2024							
Third Semester							
Computer Science and Business system							
	21UM	IA327- DISCRETE N	IATHEMATICS AND	CACULUS			
		(Regul	ations 2021)				
Dur	ation: Three hours			Maximum	: 100 Marks		
Answer All Questions							
	PART A - $(10x \ 1 = 10 \ Marks)$						
1.	1. The truth value "If 71 is prime then 3 is even", The truth value "1 > 3 and 3 CO1-U is a positive integer "						
	(a) T,F	(b) F,T	(c) T,T	(d) F,F			
2.	$P \rightarrow \neg Q$ is equivalent	nt to			CO6- U		
	(a) $\neg P \land Q$	(b) $P \land \neg Q$	(c) $\neg (P \land Q)$	(d) $P \lor \cdot$	$\neg Q$		
3.	3. If a bit string contains {0, 1} only, having length 5 has no more than 2 ones CO2- App in it. Then calculate how many such bit strings are possible?						
	(a)14	(b)12	(c)16	(d)12			
4.	Calculate how many integers between 1 to250 are divisible by 2 or 3 CO2- App						
	(a) 41	(b)167	(c)83	(d) 174			
5.	A subgroup of the g	roup $\{1, \omega, \omega^2\}$ where	$\omega^3 = 1$ under the m	ultiplication is	CO6- U		
	(a) $\{1, \omega\}$	(b) $\{\omega, \omega^2\}$	(c) $\{1, \omega^2\}$	(d) None	of the above		
6.	The union of two su	bgroup of G is a			CO6- U		
	(a) Subgroup	(b) semi group	(c) group	(d) Mon	oid		
7.	$\int_{0}^{\infty} e^{-x} x^{4} dx$				CO4- App		
	(a) 4	(b) 4!	(c) 5	(d) 5!			

8.	$\int_{0}^{\infty} 6e$	$e^{-x}x^5dx$				CO4- App	
	(a) 6	5	(b) 6!	(c) 7!	(d) 5!		
9.	The region of integration of the integral $\int_{0}^{1} \int_{0}^{x} f(x, y) dx dy$ is CO6-					CO6- U	
	(a) s	(a) square (b) rectangle (c) triangle (d) cit			(d) circ	rcle	
10.	The	value of integral \int_{1}^{2}	$\int_{1}^{4} \frac{dxdy}{xy}$			CO5- App	
	(a) 1	log 8	(b) $(\log 2)^2$	(c) $\log 6$ (d) None of t	he above	
			PART – B (5 x 2	= 10Marks)			
11.	Compute PDNF for $(P \lor Q)$ CO1-					CO1- App	
12.	In how many ways can letters of the word "THUNAIEZHUTHU" be CO2- App arranged						
13.	For a Group $G = \{1, -1, -i, i\}$ under multiplication, Find order of all elements CO3- App						
14.	Compute y_{25} if $y = \frac{1}{x}$					CO4- App	
15.	Solve $\int_{0}^{1} \int_{0}^{2} x^2 y^2 dy dx$				CO5- App		
PART – C (5 x 16= 80Marks)							
16.	(a)	(i) Calculate PC	NF and PDNF for $(P \land -$	$\neg Q) \lor (P \land R) \lor (Q \land R)$) CO1	-App (8)	
			es of inference derive &	-	CO1	-App (8)	
	$P \to (Q \to V), \neg U \lor P, Q \Rightarrow U \to (V \land P)$						
	(b)	(i) Prove the follo	Or owing by Indirect Meth	od.	CO1	-App (8)	
			$(S) \to U, P \lor S \Rightarrow U$				
		to write program write programs	e premises "one studen s in JAVA"and "Every in JAVA can get a hig e one in this class can	y one who knows ho h- paying jop" imply	w to	-App (8)	

17.	(a)	(i) Using mathematical induction show that	CO2 -App	(8)
		$n^{3} + (n+1)^{3} + (n+2)^{3}$ is a multiple of 9.	CO2 4	(0)
		(ii) Solve $a_n - 4a_{n-1} + 4a_{n-2} = 2^n, a_0 = 1, a_1 = 1$.	CO2 -App	(8)
		Or		
	(b)	(i) Calculate the number of positive integers not exceeding 1200 that are divisible by 2,3,5 or by 7	CO2 -App	(8)
		(ii) Using generating functions Solve $a_n = 3a_{n-1} + 5^n$, $a_0 = 4$	CO2 -App	(8)
18.	(a)	(i) Let G be a finite group of order 'n' and H be any subgroup of G. Then Show that the order of H divides the order of G. (i.e) $O(H) / O(G)$	CO3- App	(8)
		(ii) Show that $(Q^+,*)$ is ab abelian Group. Where * defined as	CO3- App	(8)
		$a^*b = \frac{ab}{2}$ where $a, b \in Q^+$		
		Or		
	(b)		CO3- App	(16)
		(a,b)*(x,y) = (ax,ay+b)		
		 (i) Prove that (S, *) is a semi group (ii) Is it commutative and calculate the value of (2.4)*(1.5) 		
		(ii). Is it commutative and calculate the value of (2,4)*(1,5)(iii) Find the identity Element		
		(iv) Find the inverse of $(2,3)^*(8,6)$ and $(0,2)^*(3,5)$		
19.	(a)	(i) If $y = a \cos(\log x) + b \sin(\log x)$ Show that $x^2 y_1 + x y_1 + y = 0$	CO4-App	(8)
		(ii) Compute the value of a,b,c if $\lim_{x \to 0} \frac{ae^x - be^{-x} - cx}{x - \sin x} = 4$	CO4-App	(8)
		Or .		
	(b)	(i) Compute $\int_{0}^{\frac{\pi}{2}} \frac{dx}{1 + \sqrt{\tan x}}$	CO4-App	(8)
		(ii) Evaluate $\lim_{x \to 0} \frac{xe^x - \log(1+x)}{x^2}$	CO4-App	(8)

20. (a) (i) Find the volume of the tetrahedron bounded by CO5- App (8) 6x + 4y + z = 12, x = 0, y = 0, z = 0.(ii) Compute the area between the parabola $y^2 = x$ and $x^2 = y$ CO5- App (8) Or (b) (i) Evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1-x^2-y^2}} \int_{0}^{\sqrt{1-x^2-y^2}} \frac{dxdydz}{\sqrt{1-x^2-y^2-z^2}}$ CO5- App (8)

(ii) Change the order of integration and hence evaluate CO5- App (8)

$$\mathbf{a} \quad \mathbf{a} + \sqrt{\mathbf{a}^2 - \mathbf{y}^2}$$
$$\int \qquad \int \mathbf{x} \mathbf{y} \, \mathbf{d} \, \mathbf{x} \, \mathbf{d} \, \mathbf{y}$$
$$0 \quad \mathbf{a} - \sqrt{\mathbf{a}^2 - \mathbf{y}^2}$$