

Reg. No. :

Question Paper Code : 95400

5 Year M.Sc. DEGREE EXAMINATION, NOVEMBER/DECEMBER 2015.

Fifth Semester

Software Engineering

XCS 352/10677 SW 505 — THEORY OF COMPUTATION

(Common to 5 Year M.Sc. Computer Technology and M.Sc. Information Technology)

(Regulations 2003/2010)

Time : Three hours

Maximum : 100 marks

Answer ALL questions.

PART A — (10 × 2 = 20 marks)

1. Define pumping lemma for regular languages.
2. Show the equivalence between regular expression and finite automata.
3. Write a CFG to generate the set $\{a^m b^n c^p / m + n = p \text{ and } p \geq 1\}$.
4. For the grammar $S \rightarrow aCa, C \rightarrow aCa / b$, find $L(G)$.
5. Explain the components of a TM with a neat diagram.
6. Differentiate between PDA Vs TM.
7. Mention any two undecidable problems.
8. Is the problem of type 0 grammar unsolvable? Justify your answer.
9. Prove that P is closed under complement.
10. Give two applications of NP class problems.

PART B — (5 × 16 = 80 marks)

11. (a) (i) Define regular expression and regular languages. What language is represented by the regular expression $(c^* (a \cup (bc^*))^*)$? (8)
- (ii) What are the properties that are closed under regular languages? Give examples of each. (8)

Or

- (b) Construct a non-deterministic finite automata accepting the regular expression $(ab \cup aab \cup aba)^* a$. Design an equivalent deterministic finite automata that accepts the regular expression and trace for a string $w = aababaa$.
12. (a) Prove any four closure properties of context free grammar.

Or

- (b) (i) Prove that L is $L(M_2)$ for some PDA M_2 iff L is $N(M_1)$ for some PDA M_1 .
- (ii) Construct a PDA by empty stack for $L = \{a^n b^n / n \geq 1\}$.
13. (a) (i) Show that the single tape Turing machine can be simulated to multitape Turing machine in solving any problem. Illustrate with an example. (8)
- (ii) Define an unrestricted grammar. Construct a unrestricted grammar for the language $\{a^n b^m c^n d^m \mid n \neq m \text{ and } n, m \geq 1\}$. (8)

Or

- (b) Elaborate on recursive and recursively enumerable language, related to concepts, relationships and properties.
14. (a) (i) Show that halting problem of TM is undecidable. (8)
- (ii) State and prove the Rice theorem. (8)

Or

- (b) Explain the universal Turing machine as an undecidable problem.

15. (a) State and explain any one of the following NP-Complete problem.

- (i) Travelling salesman problem
- (ii) Subgraph isomorphism problem.

Or

(b) (i) Write the characteristic features of P-completeness. Explain with an example. (12)

(ii) How is time complexity and space complexity defined in NP and P problems? (4)
