

Reg. No.:												
-----------	--	--	--	--	--	--	--	--	--	--	--	--

Question Paper Code: 71687

B.E./B.Tech. DEGREE EXAMINATION, APRIL/MAY 2015.

Sixth Semester

Electrical and Electronics Engineering

IC 2351/IC 61/10133 IC 604 — ADVANCED CONTROL SYSTEM

(Common to Instrumentation and Control Engineering)

(Regulation 2008/2010)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

$$PART A - (10 \times 2 = 20 \text{ marks})$$

- 1. Mention the limitations of conventional control theory.
- 2. What is an observer? Under what conditions would you use an observer in your feedback design of a control system?
- 3. List the common physical non linearities present in a system.
- 4. Write the drawback of phase plane method.
- 5. What are the assumptions to be considered for describing function analysis of steady-state oscillations in non linear systems?
- 6. Define limit cycle.
- 7. Test the asymptotic stability using Liapunav's direct method for the system of dynamics.

$$\dot{\mathbf{y}} = \begin{bmatrix} -1 & -2 \\ 1 & -4 \end{bmatrix} \mathbf{y}$$

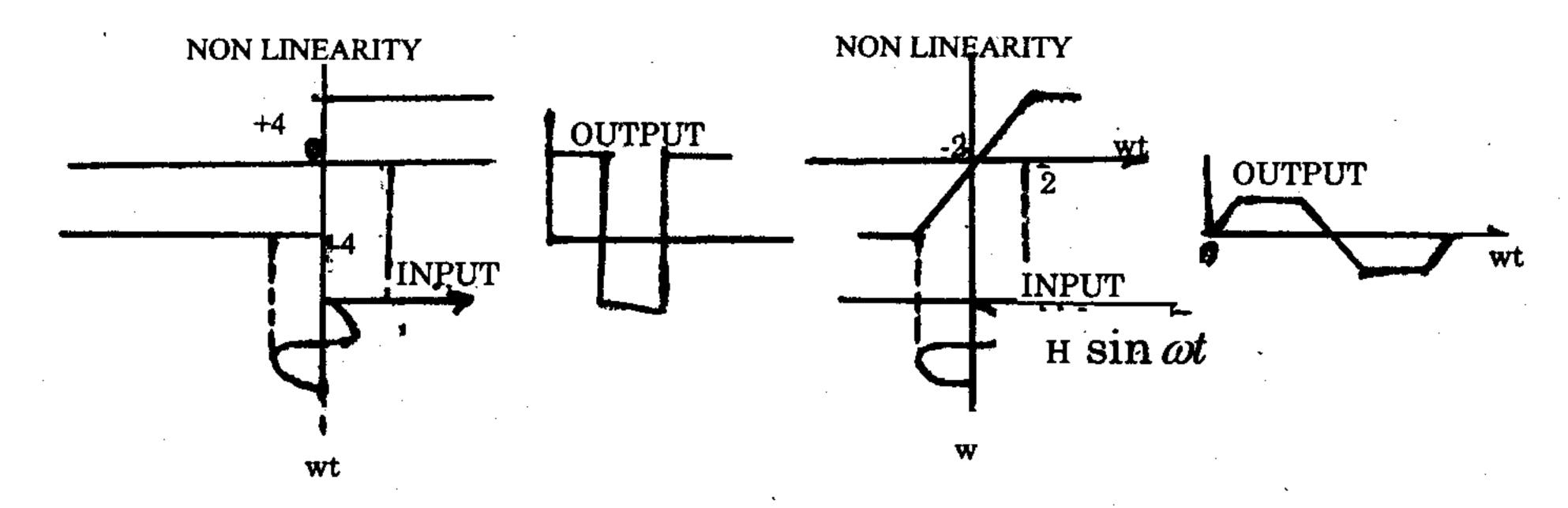
- 8. State Popov's criterion.
- 9. Mention the factors to be considered for designing an optimal controller.
- 10. What is a singular minimum time problem?

PART B —
$$(5 \times 16 = 80 \text{ marks})$$

11. (a) A system is described by $\frac{d^3y}{dt^3} + \frac{6dy^2y}{dt^2} + \frac{11dy}{dt} + 2y = 6u$ where y is the output and u is the input of the system. Obtain the state space representation of the system and check for its controllability and observability. (16)

The dynamics of the system is represented by $\dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$ and output $y = \begin{bmatrix} 2 & 0 \end{bmatrix} x$ with the initial conditions $x(0) = \begin{bmatrix} 0.5 & 0 \end{bmatrix}^T$. Design a state observer, so that the new pole placement will be at (-10, -10). (16)

- 12. (a) Construct a phase plane portrait of the control system described by the following derivative equation $\ddot{x} + 0.5\dot{x} + 2x + x^2 = 0$. (16)
 - (b) Discuss the algorithm of constructing the phase portrait by isocline method with example. (16)
- 13. (a) Illustrate the idealized characteristics of a non linearity having deadzone and its response due to sinusoidal input. (16)
 - (b) Find out the describing function for the system shown in figure. (16)



14. (a) (i) Verify that

 $V = x_1^4 + 2x_2^2 + 2x_1 + x_2 + x_1^2$ is a Liapunov function for the system describe by the equation $\frac{dx_1}{dt} = x_2, \frac{dx_2}{dt} = -x_2 - x_1^3$. (8)

(ii) The differential equation of a nonlinear device is

 $\frac{d^2x}{dt^2} + 2x^2 \frac{dx}{dt} + x = 0.$ Use Liapunov's method to determine its stability. (8)

Or

(b) State and prove Liapunovs stability theorem. Also explain what the sufficient conditions of stability. (16)

15. (a) Consider a first order system described by the differential equation $\dot{x}(t) = 2x(t) + u(t)$. Find the optimal control law that minimizes the

performance index
$$J = \frac{1}{2} \int_{0}^{t_{f}} \left(3x^{2} + \frac{1}{4}u^{2} \right) dt, t_{f} = 1 \sec$$
 (16)

Or

(b) Consider a plant to be controlled which is described by a state space model.

$$\dot{x}(t) = Ax(t) + Bu(t)$$

$$y(t) = Cx(t)$$

Outline the process by which you would design a discrete LQ regulator incorporating a current state estimator. (16)