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**Question Paper Code: 55024**

B.E. / B.Tech. DEGREE EXAMINATION, NOV 2017

Fifth Semester

Computer Science and Engineering

15UCS504 - THEORY OF COMPUTATION

(Regulation 2015)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (5 x 1 = 5 Marks)

- Given an arbitrary non-deterministic finite automaton (NFA) with  $N$  states, the maximum number of states in an equivalent DFA.  
(a)  $N^2$                       (b)  $2^N$                       (c)  $2N$                       (d)  $N!$
- Let  $L = \{0^n \mid n \text{ is a perfect square}\}$ . Then language  $L$  is  
(a) Context free              (b) Regular                      (c) Not Regular              (d) Recursive
- The language generated by the grammar  $S \rightarrow aSa|bSb|a|b$  over the alphabet  $\{a, b\}$  is the set of  
(a) All palindrome                      (b) All odd length palindromes  
(c) All even length palindromes              (d) Strings that begin and end with 'a' or 'b'
- Context free languages are not closed under which of the following operation.  
(a) Union                                      (b) Intersection  
(c) Concatenation                              (d) Closure
- If  $L$  and  $L'$  are recursively enumerable, then  $L$  is  
(a) Context free                                      (b) Regular  
(c) Context sensitive                                      (d) Recursive

PART - B (5 x 3 = 15 Marks)

6. Design a DFA to accept the language  $L = \{ w \mid w \text{ has both an even number of } 0\text{'s and even number of } 1\text{'s} \}$ ?
7. State the pumping lemma for regular language.
8. For the grammar  $S \rightarrow aCa, C \rightarrow aCa/b$ . Find  $L(G)$ .
9. Define the acceptance of PDA by empty stack. Is it true that the language accepted by a PDA by empty stack is equivalent to the language accepted by a PDA by final state.
10. State the closure properties of recursive and recursively enumerable languages.

PART - C (5 x 16 = 80 Marks)

11. (a) (i) Compare DFA and NFA with examples. (6)
- (ii) Construct DFA equivalent to the NFA given below (10)

	0	1
p	{p,q}	{p}
q	{r}	{r}
r	{s}	$\phi$
*s	{s}	{s}

Or

- (b) (i) Construct the deterministic finite automata to accept string of 0's and 1's ending with the string 011. (8)
  - (ii) Prove that a language accepted by some NFA if and only if L is accepted by DFA. (8)
12. (a) Construct a minimized DFA for the regular expression  $(a|b)^*abb$ . (16)

Or

- (b) (i) Prove that the language  $L = \{ 0^n 1^n \mid n \geq 1 \}$  is not regular. (8)
  - (ii) Explain any three closure properties of Regular languages. (8)
13. (a) (i) Let G be a grammar  $S \rightarrow 0B|1A, A \rightarrow 0|0S|1AA, B \rightarrow 1|1S|0BB$ . For the string 00110101 find its leftmost derivation and derivation tree. (8)

(ii) Prove that the following grammar is ambiguous.  $S \rightarrow aS \mid aSbS \mid \epsilon$ . (8)

Or

(b) Define Chomsky Normal Form (CNF). Convert the following grammar to CNF.

$S \rightarrow AB \mid aB$

$B \rightarrow aab \mid \epsilon$

$B \rightarrow bbA$

(16)

14. (a) (i) Construct a PDA accepting by empty stack for the language

$L = \{a^m b^m c^n \mid m, n \geq 1\}$ . (8)

(ii) If P be a PDA. Then there is a context free grammar G such that  $L(G) = L(P)$ . (8)

Or

(b) (i) Find the PDA equivalent to the given CFG with the following productions

$S \rightarrow aB \mid bA, A \rightarrow a \mid aS \mid bAA, B \rightarrow b \mid bS \mid aBB$ . (8)

(ii) State and prove the pumping lemma for context free language. (8)

15. (a) (i) Explain the programming techniques for Turing machine. (8)

(ii) Prove the following theorem 'If both a language L and its complement are RE, then L is recursive'. (8)

Or

(b) State and prove post's correspondence problem. (16)

