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**Question Paper Code: 41254**

B.E. / B.Tech. DEGREE EXAMINATION, MAY 2017

Fifth Semester

Computer Science and Engineering

14UCS504 – THEORY OF COMPUTATION

(Regulation 2014)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

- Any NFA can be converted to a DFA
  - always
  - never
  - depending on the NFA
  - depending on the language of NFA
- What is the minimum number of states in a DFA that recognizes the set of all binary strings which contains four consecutive 1's?
  - 6
  - 5
  - 4
  - 3
- Pumping lemma is generally used for proving
  - A given grammar is regular
  - A given grammar is not regular
  - Whether two given regular expressions are equivalent or not
  - None of these
- The finite automata accept which of the following language.
  - context free language
  - regular language
  - context sensitive language
  - all the above
- How many tuples are needed to represent an instantaneous description of a PDA?
  - 1
  - 2
  - 3
  - 4

6. The language  $\{a^m b^n c^{m+n} \mid m, n \geq 1\}$  is
- (a) regular language (b) context free language  
(c) content sensitive but not context free (d) type-0 but not context sensitive
7. While converting the context free grammar into Greibach normal form, which of the following is not necessary?
- (a) elimination of null production  
(b) elimination of unit production  
(c) converting given grammar in Chomsky normal form  
(d) none of these
8. A PDM behaves like a TM when the number of auxiliary memory it has, is
- (a) 0 (b) 1 or more (c) 2 or more (d) all the above
9. What is the maximum number of codes is generated to encode a turing machine which consists of four transition function?
- (a) 12 (b) 24 (c) 36 (d) 48
10. The diagonalization language  $L_d$  is
- (a) recursive (b) not recursively enumerable  
(c) recursively enumerable (d) both (a) and (c)

PART - B (5 x 2 = 10 Marks)

11. Differentiate DFA and NFA.
12. When two states are equivalent and distinguishable.
13. Define the language generated by a PDA.
14. Define a turing machine.
15. Give some examples of NP-complete problems

PART - C (5 x 16 = 80 Marks)

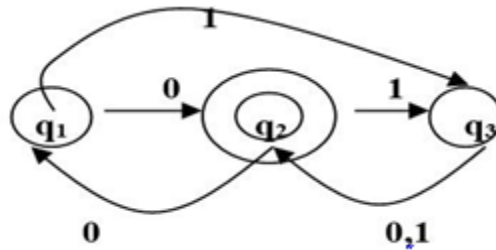
16. (a) (i) Explain the different forms of proofs with examples. (8)  
(ii) Prove that for every integer  $n \geq 0$  the number  $4^{2n+1} + 3^{n+2}$  is multiple of 13. (8)

Or

- (b) (i) Prove that if  $L$  is accepted by an NFA with  $\epsilon$  transitions, then  $L$  is also accepted by an NFA without  $\epsilon$  transitions. (8)
- (ii) Consider the following  $\epsilon$ -NFA. Compute  $\epsilon$ -closure of each state and find its equivalent DFA (8)

$\delta$	$\epsilon$	a	b	c
$\rightarrow$	$\phi$	{p}	{q}	{r}
q	{p}	{q}	{r}	$\phi$
*r	{q}	{r}	$\phi$	{p}

17. (a) Obtain the regular expression that denotes the language accepted by, using the recursive relation. (16)



Or

- (b) (i) Construct deterministic finite automata for the regular expression  $(a + b)^* ab$ . (8)
- (ii) State and prove any two closure properties of regular language. (8)
18. (a) (i) Let  $S \rightarrow aB/bA$ ,  $A \rightarrow aS/bAA/a$ ,  $B \rightarrow bS/aBB/b$ . Show that  $S \Rightarrow aaabbabbba$  and construct a derivation tree whose yield is in “ $aaabbabbba$ ”. (8)
- (ii) Construct a PDA for the language  $L = \left\{ \frac{a^n b^{2^n}}{n \geq 1} \right\}$ . (8)

Or

- (b) (i) Construct a PDA for set of palindrome over the alphabet {a, b}.  $L(M) = \{WcW^R\}$ . (8)
- (ii) Show that the following grammars are ambiguous. (8)
19. (a) (i) Discuss the closure properties of CFL and prove any one of the property. (8)
- (ii) Explain the programming techniques of turing machine. (8)

Or

(b) (i) Design a turing machine which recognizes palindrome over alphabet  $\{0, 1\}$ . (6)

(ii) Design a turing machine to compute  $f(m, n) = m * n, \forall m, n \in N$ . (10)

20. (a) (i) Prove that Lu is RE but not recursive. (8)

(ii) Obtain the code for the TM  $M = (\{q_1, q_2, q_3\}, \{0, 1\}, \{0, 1, B\}, \delta, q_1, B, \{q_2\})$   
With the moves  $\delta(q_1, 1) = (q_3, 0, R)$ ,  $\delta(q_3, 0) = (q_1, 1, R)$ ,  $\delta(q_3, 1) = (q_2, 0, R)$ ,  
 $\delta(q_3, B) = (q_3, 1, L)$ . (8)

Or

(b) (i) Define universal language  $L_u$ . Prove that  $L_u$  is recursively enumerable. (8)

(ii) State halting problem. Show that it is un-decidable. (8)

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