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**Question Paper Code: 55204**

B.E./B.Tech. DEGREE EXAMINATION, MAY 2018

Fifth Semester

Computer Science and Engineering

15UCS504 THEORY OF COMPUTATION

(Regulation 2015)

Duration: Three hours

Maximum: 100 Marks

Answer All Questions

PART A - (5x 1 = 5 Marks)

1. Given an arbitrary non-deterministic finite automaton (NFA) with  $N$  states, the maximum number of states in an equivalent DFA. CO1- R  
(a)  $N^2$                       (b)  $2^N$                       (c)  $2N$                       (d)  $N!$
2. A language is represented by a regular expression  $(a)^*(a + ba)$ . Which of the following string does not belong to the regular set represented by the above expression? CO2- U  
(a) aaa                      (b) aba                      (c) ababa                      (d) aa
3. Which of the following strings is not generated by the following grammar?  $S \rightarrow SaSbS|\epsilon$  CO3- R  
(a) aabb                      (b) abab                      (c) aababb                      (d) aaabb
4. Consider a language  $L$  for which there exists a Turing machine  $T$ , that accepts every word in  $L$  and either rejects or loops for every word that is not in  $L$ . The language  $L$  is CO4- R  
(a) NP Hard                      (b) NP Complete                      (c) recursive                      (d) recursively enumerable

5. A Turing Machine represented by a transition table has entry 1Lq4 corresponding to q3-row and 0-column then which of the following statement is false CO5- R
- (a) the symbol under read/write head is 0 (b) next state is q4
- (c) q3 is the initial state (d) all of the above

PART – B (5 x 3= 15Marks)

6. Design a DFA that accepts the language over the alphabet {0, 1} and that has the set of all strings with 011 as a substring. CO1- U
7. State the pumping lemma for Regular languages. CO2- U
8. For the grammar  $S \rightarrow aCa, C \rightarrow aCa/b$ . Find  $L(G)$ . CO3- U
9. Show that, for arbitrary context free grammar  $G_1$  and  $G_2$ , the problem “ $L(G_1) \cap L(G_2)$  is Context free” is undecidable. CO4- U
10. Design a Turing Machine that can accept the language denoted by regular expression  $11^*$ . CO5- U

PART – C (5 x 16= 80Marks)

11. (a) Consider the following  $\epsilon$ -NFA. Compute the  $\epsilon$ -Closure of each state and find its equivalent DFA. CO1-Ana (16)

State/Input	$\epsilon$	a	b	c
s				
$\rightarrow P$	q	p	$\Phi$	$\Phi$
q	r	$\Phi$	p	$\Phi$
$*r$	$\Phi$	$\Phi$	$\Phi$	r

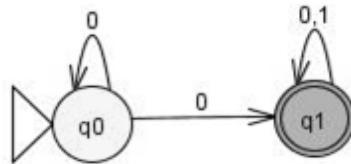
Or

- (b) Give the state diagram of a DFA (or an NFA) that accepts only binary strings which represent numbers divisible by two or three. CO1 -Ana (16)  
 E.g., it accepts 0, 00, 10, 011, but it rejects the empty string, 1, 101, 0111.

12. (a) Construct a minimized DFA for the regular expression  $(a|b)^*abb$ . CO2 -U (16)

Or

- (b) Find the regular expression corresponding to the equivalent finite automaton given below using equation method  $R_{ij}^{(k)}$  CO2 -U (16)



13. (a) Begin with the grammar  $S \rightarrow 0A0 | 1B1 | BB$ ;  $A \rightarrow C$ ;  $B \rightarrow S|A$ ;  $C \rightarrow S|\epsilon$  CO3- App (16)  
and simplify using the safe order  
(i) Eliminate  $\epsilon$ -Productions  
(ii) Eliminate unit productions  
(iii) Eliminate useless symbols  
(iv) Put the resultant grammar in Chomsky Normal Form?

Or

- (b) Construct the grammar for the following PDA. CO3- App (16)  
 $M = (\{q_0, q_1\}, \{0, 1\}, \{X, z_0\}, \delta, q_0, Z_0, \Phi)$  and where  $\delta$  is given by

$$\begin{aligned} \delta(q_0, 0, Z_0) &= \{(q_0, XZ_0)\}, & \delta(q_0, 0, X) &= \{(q_0, XX)\}, \\ \delta(q_0, 1, X) &= \{(q_1, \epsilon)\}, & \delta(q_1, 1, X) &= \{(q_1, \epsilon)\}, \\ \delta(q_1, \epsilon, X) &= \{(q_1, \epsilon)\}, & \delta(q_1, \epsilon, Z_0) &= \{(q_1, \epsilon)\} \end{aligned}$$

14. (a) Explain how the multiple tracks in a Turing Machine can be used for testing given positive integer is a prime or not. CO4-Ana (16)

Or

- (b) Construct a Turing Machine that accepts the language  $L = \{0^n 1^n 2^n | n \geq 1\}$  using checking off symbols technique. CO4 -App (16)

15. (a) Define Computational Complexity? Explain whether the class of Problems that can be solved in polynomial time is equivalent to the class of non-deterministic polynomial problems i.e whether  $P=NP$ ? CO5- U (16)

Or

- (b) State and prove post's correspondence problem. CO5- U (16)

