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B.E./B.Tech. DEGREE EXAMINATION, NOVEMBER/DECEMBER 2013.

Sixth Semester

Computer Science and Engineering

MA 2264/MA 41/MA 51/080280026/10177 MA 401/10144 CSE 21/10144 ECE 15 — NUMERICAL METHODS

(Common to Sixth Semester – Electronics and Communication Engineering and Information Technology Fifth Semester – Polymer Technology, Chemical Engineering and Polymer Technology Fourth Semester – Aeronautical Engineering, Civil Engineering, Electrical and Electronics Engineering and Mechatronics Engineering)

(Also common to Fourth Semester MA 1251 – Numerical Methods for Civil Engineering, Aeronautical Engineering and Electrical and Electronics Engineering)

(Regulation 2008/2010)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

$$PART A - (10 \times 2 = 20 \text{ marks})$$

- 1. What do you mean by the order of convergence of an iterative method for finding the root of the equation f(x)=0?
- 2. Solve the equations x + 2y = 1 and 3x 2y = 7 by Gauss-Elimination method.
- 3. State Newton's forward difference formula for equal intervals.
- 4. Find the divided differences of $f(x) = x^3 x^2 + 3x + 8$ for the arguments 0, 1, 4, 5.
- 5. Evaluate $\int_{-2}^{2} e^{\frac{-x}{2}} dx$ by Gauss two point formula.
- 6. Evaluate $\int_{0}^{6} \frac{dx}{1+x^{2}}$ using Trapezoidal rule.

- State Adam's Predictor-Corrector formula.
- Using Euler's method find the solution of the initial value problem 8. $y' = y - x^2 + 1$, y(0) = 0.5 at x = 0.2 taking h = 0.2.
- Write the diagonal five point formula for solving the two dimensional Laplace equation $\nabla^2 u = 0$.
- Using finite difference solve y'' y = 0 given y(0) = 0, y(1) = 1, n = 2. 10.

PART B —
$$(5 \times 16 = 80 \text{ marks})$$

- Solve the equations by Gauss-Seidel method of iteration. 11. (a) 10x + 2y + z = 9, x + 10y - z = -22, -2x + 3y + 10z = 22.
 - Determine the largest eigen value and the corresponding eigen (11)vector of the matrix $\begin{pmatrix} 1 & 3 & -1 \\ 3 & 2 & 4 \\ -1 & 4 & 10 \end{pmatrix}$ with $\begin{pmatrix} 1 & 0 & 0 \end{pmatrix}^T$ as the initial (8) vector by power method.

Or

- Find the inverse of the matrix $\begin{pmatrix} 3 & -1 & 1 \ -15 & 6 & -5 \ 5 & -2 & 2 \end{pmatrix}$ using Gauss-Jordan (b) (8)
 - Using Newton's method, find the real root of $x \log_{10} x = 1.2$ correct (8)to five decimal places.
- Find the natural cubic spline to fit the data:

f(x): -1 3 29

Hence find f(0.5) and f(1.5).

method.

(16)

Or

The following table gives the values of density of saturated water (b) **(1)** for various temperatures of saturated steam. (8)

Temperature °C: 100 150 200 250 300

799 712 865 958 917 Density hg/m³:

Find by interpolation, the density when the temperature is 275°.

Use Lagrange's formula to find the value of y at x = 6 from the (8)following data:

- 13. (a) (i) Apply three point Gaussian quadrature formula to evaluate $\int_{0}^{1} \frac{\sin x}{x} dx$. (8)
 - (ii) Find the first and second order derivatives of f(x) at x = 1.5 for the following data:

x: 1.5 2.0 2.5 3.0 3.5 4.0

f(x): 3.375 7.000 13.625 24.000 38.875 59.000

(b) (i) The velocities of a car running on a straight road at intervals of 2 minutes are given below:

Time (min): 0 2 4 6 8 10 12

Velocity (km/hr): 0 22 30 27 18 7 0

Using Simpson's $\frac{1}{3}$ -rd rule find the distance covered by the car. (8)

- (ii) Evaluate $\int_{2}^{2.4} \int_{4}^{4.4} xy \ dx \ dy$ by Trapezoidal rule taking h = k = 0.1. (8)
- 14. (a) (i) Obtain y by Taylor series method, given that y' = xy + 1, y(0)=1, for x = 0.1 and 0.2 correct to four decimal places. (8)
 - (ii) Use Milne's method to find y(0.8), given $y' = \frac{1}{x+y}$, y(0) = 2y(0.2) = 2.0933, y(0.4) = 2.1755, y(0.6) = 2.2493. (8)
 - (b) Using Runge-Kutta method of order four, find y when x = 1.2 in steps of 0.1 given that $y' = x^2 + y^2$ and y(1)=1.5. (16)
- 15. (a) By iteration method solve the elliptic equation $u_{xx} + u_{yy} = 0$ over the square region of side 4, satisfying the boundary conditions.
 - (i) $u(0, y)=0, 0 \le y \le 4$
 - (ii) $u(4, y)=8+2y, 0 \le y \le 4$
 - (iii) $u(x, 0) = \frac{x^2}{2}, 0 \le x \le 4$
 - (iv) $u(x, 4)=x^2, 0 \le x \le 4$

Compute the values at the interior points correct to one decimal with h=k=1. (16)

Or

- (b) (i) Using Crank-Nicolson's scheme, solve $16\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$, 0 < x < 1, t > 0 subject to u(x, 0) = 0, u(0, t) = 0, u(1, t) = 100t. Compute u for one step in t direction taking $h = \frac{1}{4}$. (8)
 - (ii) Solve $u_{tt} = u_{xx}$, 0 < x < 2, t > 0 subject to u(x, 0) = 0, $u_t(x, 0) = 100(2x x^2)$, u(0, t) = 0, u(2, t) = 0, choosing $h = \frac{1}{2}$ compute u for four time steps. (8)