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Question Paper Code: 34021

B.E. / B.Tech. DEGREE EXAMINATION, NOV 2018

Fourth Semester

Computer Science and Engineering

01UMA421 - APPLIED STATISTICS AND QUEUEING NETWORKS

(Common to Information Technology)

(Statistical table is permitted)

(Regulation 2013)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions.

PART A - (10 x 2 = 20 Marks)

1. The density function of a continuous random variable X is

$$f(x) = \begin{cases} k(1-x^2) & 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$

Find the value of K .

2. State the axioms of probability.

3. The joint p.d.f of the two dimensional random variable (X, Y) is given by

$$f(x, y) = \frac{8xy}{9}, 1 \leq x \leq y \leq 2. \text{ Find the marginal density function } x \text{ and } y.$$

4. Show that $Cov^2(x, y) \leq Var(x).Var(y)$.

5. What are the basic principles of Design of Experiments?

6. Write any two differences between RBD and CRD.

7. Define a steady state condition.

8. What are the characteristics of queueing system?
9. Explain Tandem queue model.
10. Define Open and Closed queueing networks.

PART - B (5 x 16 = 80 Marks)

11. (a) (i) The distribution function of a random variable is given by
 $F(x) = 1 - (1+x)e^{-x}$ for $x \geq 0$. Find the density function, mean and variance. (8)
- (ii) The number of monthly breakdown of a computer is a random variable having a Poisson distribution with mean equal to 1.8. Find the probability that this computer will function for a month
- (a) without a breakdown
 - (b) with only one breakdown
 - (c) with atleast one breakdown (8)

Or

- (b) In a large consignment of electric bulb 10% are defective random sample of 20 is taken for inspection. Find the probability that (1) All are good bulbs (2) At most there are 3 defective bulbs (3) Exactly there are 3 defective bulbs. (16)

12. (a) (i) The random variable [X, Y] has the following joint p.d.f

$$f(x, y) = \begin{cases} \frac{x+y}{2}, & 0 \leq x \leq 2, 0 \leq y \leq 2 \\ 0 & , otherwise \end{cases}$$

Obtain the marginal distribution of X and Y and compute co variance [X, Y]. (8)

- (ii) 20 dice are thrown. Find approximately the probability that the sum obtained is between 65 and 75 using central limit theorem. (8)

Or

- (b) (i) Obtain the equation of the lines of regression for the following data (8)

| | | | | | | | | |
|---|----|----|----|----|----|----|----|----|
| X | 65 | 66 | 67 | 67 | 68 | 69 | 70 | 72 |
| Y | 67 | 68 | 65 | 68 | 72 | 72 | 69 | 71 |

(ii) The joint probability mass function of X and Y is given below

| | | |
|------------------|---------------|---------------|
| $x \backslash y$ | -1 | 1 |
| 0 | $\frac{1}{8}$ | $\frac{3}{8}$ |
| 1 | $\frac{2}{8}$ | $\frac{2}{8}$ |

Find correlation coefficient of (X, Y) . (8)

13. (a) The following is a Latin square of a design, when 4 varieties of seeds are being tested. Set up the analysis of variance table and state your conclusion. (16)

| | | | |
|------|------|------|------|
| A105 | B95 | C125 | D115 |
| C115 | D125 | A105 | B105 |
| D115 | C95 | B105 | A115 |

Or

(b) Analyse the variance in the following Latin square of yields (in kgs) of paddy where A, B, C, D denote the different methods of cultivation

| | | | |
|------|------|------|------|
| D122 | A121 | C123 | B122 |
| B124 | C123 | A122 | D125 |
| A120 | B119 | D120 | C121 |
| C122 | D123 | B121 | A122 |

Examine whether the different methods of cultivation have given significantly different yields. (16)

14. (a) Honda auto service station has 5 mechanics, each of whom can service a motorbike in 2 hours on an average. The motorbikes are registered at a single counter and then sent for servicing to different mechanics. Motorbikes arrive at the service station at an average rate of 2 per hour. Determine

- (i) Probability that the system shall be idle,
- (ii) Probability that there shall be 3 and 8 motorbikes in the station,
- (iii) Expected number of motorbikes in the service station and queue,
- (iv) Average waiting time in the queue,
- (v) Average time spent by a motorbike in waiting and getting serviced. (16)

Or

- (b) Honda auto service station has 5 mechanics, each of whom can service a motorbike in 2 hours on an average. The motorbikes are registered at a single counter and then sent for servicing to different mechanics. Motorbikes arrive at the service station at an average rate of 2 per hour. Determine
- (i) Probability that the system shall be idle,
 - (ii) Probability that there shall be 3 and 8 motorbikes in the station,
 - (iii) Expected number of motorbikes in the service station and queue,
 - (iv) Average waiting time in the queue,
 - (v) Average time spent by a motorbike in waiting and getting serviced. (16)

15. (a) Derive the expected steady state system size for the single server system with Poisson input and general service (Pollaczek-Khintchine formula). (16)

Or

- (b) In a network of 3 service stations 1,2,3 customers arrive 1,2,3 from outside, in accordance with Poisson process having rates 5, 10,15 respectively. the service times at the 3 stations are exponential with respective rates 10,50, 100. A customer completing service at station 1 is equally like to (1) go to station 2, (2) go to station 3 and (3) leave the system. A customer departing from service at station 2 always goes to station 3. A departure from service at station at station 3 is equally like to go to station 2 or leave the system. Then
- (i) What is the average number of customers in the system consisting of all the three stations?
 - (ii) What is the average time a customer spends in the system? (16)