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Question Paper Code: 41204

B.E. / B.Tech. DEGREE EXAMINATION, NOV 2016

Fifth Semester

Computer Science and Engineering

14UMA521 - DISCRETE MATHEMATICS

(Regulation 2014)

(Common to IT Branch)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

- Which of the following statement is the negation of the statement “The crop will be destroyed if there is a flood” ?
 - The crop will not be destroyed, if there is a flood
 - The crop will not be destroyed, if there is no flood
 - Crops are destroyed during the flood
 - There is a flood and the crops are not destroyed
- $P \rightarrow Q$ is equivalent to
 - $\neg Q \rightarrow P$
 - $Q \rightarrow P$
 - $P \rightarrow \neg Q$
 - $\neg Q \rightarrow \neg P$
- In how many different ways can the letters of the word 'LEADING' be arranged in such a way that the vowels always come together?
 - 620
 - 710
 - 720
 - 610
- Solve for n: $a^n P_2 = 42$
 - 2
 - 6
 - 4
 - 42
- A vertex of degree one is called
 - Isolated vertex
 - Unit vertex
 - Pendant vertex
 - Proper vertex

6. Indicate which one of the following five graphs $G = (V, E, f)$, $|V| = 5$, is not connected
- (a) $f = \{\{1,2\}\{1,2\}\{2,3\}\{3,4\}\{1,5\}\{1,5\}\}$ (b) $f = \{\{1,2\}\{2,3\}\{1,2\}\{1,3\}\{2,3\}\{4,5\}\}$
(c) $f = \{\{1,2\}\{2,3\}\{1,2\}\{2,3\}\{3,4\}\{1,5\}\}$ (d) $f = \{\{4,5\}\{1,3\}\{1,3\}\{2,3\}\{2,4\}\{4,5\}\}$
7. The set of all real number usual multiplication is not a group, since
- (a) Multiplication is not a binary operation (b) Multiplication is not associative
(c) Identity element does not exist (d) Zero has no inverse
8. Match the following:
- | | |
|-------------------|--------------------|
| 1. Groups | I. Associativity |
| 2. Semi Groups | II. Identity |
| 3. Monoids | III. Commutativity |
| 4. Abelian Groups | IV. Left Inverse |
- (a) III I IV II (b) IV I II III
(c) II III I IV (d) I II III IV
9. A self-complimented, distributive lattice is called
- (a) Modular Lattice (b) Boolean Algebra
(c) Complete Lattice (d) Self-Dual Lattice
10. Let $D_{30} = \{1, 2, 3, 4, 5, 6, 10, 15, 30\}$ and relation / (divides) be partial ordering on D_{30} . Then the least upper bound (lub) of 10 and 15 is
- (a) 30 (b) 15 (c) 10 (d) 6

PART - B (5 x 2 = 10 Marks)

11. Using truth table, show that $P \vee \neg (P \wedge Q)$ is tautology.
12. Find the recurrence relation from $y_k = A2^k + B3^k$.
13. Give an example of a graph which is both Eulerian and Hamiltonian.
14. Draw all the spanning trees of K_3 .
15. Let $A = \{a, b, c\}$ and $\rho(A)$ be its power set. Draw the Hasse diagram of $(\rho(A), \subseteq)$.

PART - C (5 x 16 = 80 Marks)

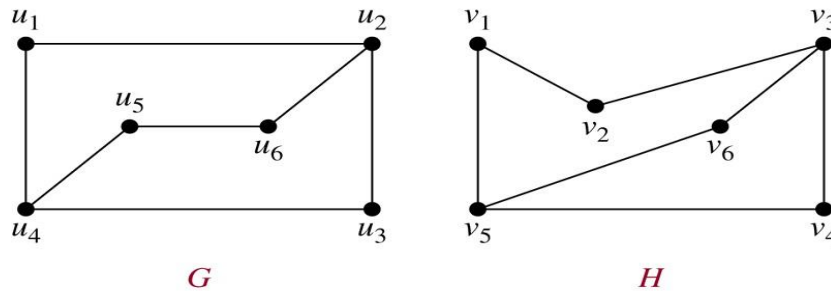
16. (a) (i) Without using the truth table, find the PCNF and PDNF of the statement $(\neg P \rightarrow R) \wedge (Q \leftrightarrow P)$.
- (8)
- (ii) Show that $(\forall x)(P(x) \vee Q(x)) \Rightarrow (\forall x)P(x) \vee (\exists x)Q(x)$. (8)

Or

- (b) (i) Check whether the following set of premises are not valid: Whenever the system software is being upgraded, users cannot access the file system. If users can access the file systems, then they can save new files. If users cannot save new files, then the system software is not being upgraded. (8)
- (ii) Show that $(\exists x)(P(x) \rightarrow Q(x))$ follows from the premises $\exists x(P(x) \wedge Q(x)) \rightarrow (y)(R(y) \rightarrow S(y))$ and $\exists y(R(y) \wedge \neg S(y))$. (8)
17. (a) (i) Solve the recurrence relation $y_{n+2} - 6y_{n+1} + 9y_n = 0$, $y_1 = 4$ and $y_0 = 1$. (8)
- (ii) Find the number of integers between 1 and 100, both inclusive, that are divisible by 2, 3, 5, but not by 7. (8)

Or

- (b) (i) Show that by mathematical induction principle, $3^{2n} + 4^{n+1}$ is divisible by 5, for $n \geq 0$. (8)
- (ii) Using generating function, solve the recurrence relation $a_{n+2} - a_{n+1} - 6a_n = 0$, given $a_0 = 2$ and $a_1 = 1$. (8)
18. (a) (i) Examine whether the following graphs are isomorphic. (8)



- (ii) Prove that a connected graph is Eulerian if all vertices are of even degree. (8)

Or

- (b) (i) Prove that a simple graph with n vertices must be connected if it has more than $\frac{(n-1)(n-2)}{2}$ edges. (8)
- (ii) Find the adjacency matrix of the following graph G . Find A^2, A^3 and $Y = A + A^2 + A^3 + A^4$. What is your observation of entries in A^2 and A^3 ? (8)
19. (a) (i) State and prove Lagrange's theorem. (8)

- (ii) Prove that intersection of two normal subgroup of $(G, *)$ is again a normal subgroup of $(G, *)$. (8)

Or

- (b) (i) Prove that a non-empty subset H of a group G is a subgroup if $a, b \in H \Rightarrow a * b^{-1} \in H$. (8)

- (ii) Let $f: G \rightarrow G$ be a homomorphism of group G with kernel K . Then prove that K is a normal subgroup of G and G/K is isomorphic to image of f . (8)

20. (a) (i) State and prove DeMorgan's law of lattice. (8)

- (ii) In any Boolean algebra, show that $a'b + ab' = 0$ iff $a = b$. (8)

Or

- (b) (i) State and prove distributive inequality of Lattice. (8)

- (ii) In a complemented, distributive lattice, prove the following:

- (i) $(ab)' + (a + b)' = a' + b'$ (ii) $ab'c + ab'c = b'c$ (8)