

Reg. No. :

--	--	--	--	--	--	--	--	--	--

**Question Paper Code: 53022**

B.E. / B.Tech. DEGREE EXAMINATION, DEC 2020

Third Semester

Computer Science Engineering

15UMA322 - PROBABILITY, STATISTICS AND QUEUEING SYSTEMS

(Common to Information Technology branch)

(Regulation 2015)

(Statistical tables are may be permitted)

Duration: One hour

Maximum: 30 Marks

PART A - (6 x 1 = 6 Marks)

**(Answer any six of the following questions)**

1. The mean and variance of the Binomial distribution are 4 and 3 respectively. Find  $P(X=0)$ . CO1- R  
(a)  $(1/4)^{16}$                       (b)  $1/4$                       (c)  $(3/4)^{16}$                       (d)  $3/4$
2. Find  $\lambda$ , if X follows Poisson Distribution such that  $P(X=2)=3P(X=3)$ . CO1- R  
(a) 3                      (b) 4                      (c) 2                      (d) 1
3.  $\text{Cov}(X, Y) =$  CO2- R  
(a)  $E(XY) - E(X)E(Y)$                       (b)  $E(X')E(Y') - E(X.Y)$   
(c)  $E(X)E(Y) - E(X.Y)$                       (d)  $E(XY) - E(X')E(Y')$
4. If X and Y are independent RVs with variances 8 and 5.find the variance of  $3X+4Y$ . CO2- R  
(a) 152                      (b) 153                      (c) 163                      (d) 162
5. The number of experimental units in the block is called as CO3- R  
(a) Block design                      (b) Block size                      (c) Complete block unit                      (d) Unit size
6. A \_\_\_\_\_ is a variable defining a categorization. CO3- R  
(a) Fixed Factor                      (b) Factor                      (c) Local Control                      (d) Error Control

7. What do the letter “d” in the symbolic representation (a/b/c): (d/e) of a queueing model represent? CO4- R
- (a) Service distribution (b) System capacity  
 (c) Arrival distribution (d) No.of. server
8. M/G/1 Queuing system is Markovian – Comment the statement CO4- R
- (a) Correct (b) Wrong (c) Partially Correct (d) None of these
9. Find the expected number of customers in the system, if  $\lambda=1/13$  and  $\mu=1/4$  in (M/M/1);( $\infty$ /FCFS) CO5- R
- (a) 0.4444 (b) 0.777 (c) 1.4444 (d) 1.04
10. The service facilities are arranged in a sequence and the flow is always in a single direction is called \_\_\_\_\_ CO5- R
- (a) Series Queue (b) Open Queue (c) Closed Queue (d) Parallel Queue

PART – B (3 x 8= 24 Marks)

**(Answer any three of the following questions)**

11. An electrical firm manufactures light bulbs that have the length of life which is normally distributed with mean of 800 hours and standard deviation of 40 hours. Find the probability that a bulb burns between 778 and 834 hours. CO1- App (8)
12. The joint probability distribution of two dimensional random variable (X,Y) is given by  $f(x,y)=\frac{1}{3}(x+y)$ ,  $0 \leq x \leq 1, 0 \leq y \leq 2$ . Find the correlation coefficient. Also find the equations of two lines of regression. CO2- App (8)
13. Analyze the following latin square experiment. CO3- Ana (8)
- |       |       |       |       |
|-------|-------|-------|-------|
| A 105 | B 95  | C 125 | D 115 |
| C 115 | D 125 | A 105 | B 105 |
| D 115 | C 95  | B 105 | A 115 |
| B 95  | A 135 | D 95  | C 115 |
14. There are three typists in an office. Each typist can type an average of 6 letters per hour. If letters arrive for being typed at the rate of 15 letters per hour. what fraction of time all the typists will be busy ? what is the average number of letters waiting to be typed? CO4- App (8)

15. Derive the Pollaczek- Khintchine formula for M/G/1 queue. Hence CO5- U (8)  
deduce the result for the queues M/D/1 and M/E<sub>k</sub>/1 as special cases.