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Question Paper Code: 50002

B.E. / B.Tech. DEGREE EXAMINATION, MAY 2017

First Semester

Civil Engineering

15UMA102 – ENGINEERING MATHEMATICS - I

(Common to ALL Branches)

(Regulation 2015)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

1. Evaluate $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3}$

(a) 0

(b) 4

(c) 1

(d) 6

2. If $x = a \cos \theta$, $y = b \sin \theta$, then $\frac{dy}{dx}$ is

(a) $\frac{-b}{a} \cot \theta$

(b) $\frac{b}{a} \cot \theta$

(c) $b \cos \theta$

(d) $b \sin \theta$

3. If U is a homogeneous function of degree 'n' then by Euler's theorem

(a) $x \frac{\partial U}{\partial x} + y \frac{\partial U}{\partial y} = U$

(b) $x \frac{\partial U}{\partial x} + y \frac{\partial U}{\partial y} = nU$

(c) $x \frac{\partial U}{\partial x} - y \frac{\partial U}{\partial y} = U$

(d) $x \frac{\partial U}{\partial x} - y \frac{\partial U}{\partial y} = nU$

4. The order of $f(x, y) = \frac{x^6 + y^6}{x^4 - y^4}$ is

(a) 3

(b) 2

(c) 1

(d) 0

5. $\int x e^x dx$ is

(a) $e^x(x + 1) + 1$

(b) $e^x(x - 1)$

(c) $e^x(1 - x)$

(d) $x e^x$

6. If $f(x)$ is odd then $\int_{-1}^1 f(x) dx$.
 (a) 2 (b) 0 (c) 1 (d) 1/2
7. Change the order of integration of $\int_0^a \int_y^a f(x,y) dx dy$ is
 (a) $\int_0^x \int_0^a f(x,y) dy dx$ (b) $\int_0^a \int_0^x f(x,y) dy dx$
 (c) $\int_0^a \int_a^x f(x,y) dy dx$ (d) $\int_0^a \int_0^y f(x,y) dy dx$
8. $\int_0^1 \int_0^2 \int_0^3 dz dy dx$ is
 (a) 0 (b) 1 (c) 2 (d) 6
9. The eigen values of $\begin{bmatrix} 5 & 6 & 17 \\ 0 & -9 & 23 \\ 0 & 0 & 37 \end{bmatrix}$ are
 (a) 5, -9, 23 (b) 6, -9, 37 (c) 17, 6, 5 (d) 5, -9, 37
10. Matrix $\begin{bmatrix} x & 2 \\ 1 & x-1 \end{bmatrix}$ is singular for $x =$
 (a) 1, 2 (b) -1, -2 (c) -1, 2 (d) 1, -2

PART - B (5 x 2 = 10 Marks)

11. If $x^3 + y^3 = 3axy$ then find $\frac{dy}{dx}$.
12. If $x = r \cos \theta, y = r \sin \theta$, then find $J(u, v)$.
13. Evaluate $\int_0^{\pi/2} \sin^6 x dx$.

14. Evaluate $\int_0^1 \int_0^2 x(x+y) dy dx$.

15. Define Cayley Hamilton theorem and its applications.

PART - C (5 x 16 = 80 Marks)

16. (a) If $y = e^{a \sin^{-1} x}$, prove that

$$(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} - (n^2 + a^2)y_n = 0 \quad (16)$$

Or

(b) Find the n^{th} derivative of $\frac{x^3}{(x-a)(x-b)(x-c)}$ (16)

17. (a) Investigate the maxima of the function $f(x, y) = x^3y^2(1 - x - y)$. (16)

Or

(b) A rectangular box open at the top is said to have a volume of 32cc. Find the dimensions of the box that requires the least material for its construction. (16)

18. (a) Prove that $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$ (16)

Or

(b) (i) Prove that $\Gamma(n + 1) = n\Gamma(n)$. (8)

(ii) Prove that $\beta\left(m, \frac{1}{2}\right) = 2^{2m-1}\beta(m, m)$. (8)

19. (a) Change the order of integration and then evaluate $\int_0^1 \int_{x^2}^{2-x} xydydx$. (16)

Or

(b) Evaluate $\int \int \int (x + y + z) dx dy dz$ over the region V, where the region V is bounded by $x + y + z = a$, $x = 0$, $y = 0$, $z = 0$. (16)

20. (a) Verify Cayley – Hamilton theorem for $A = \begin{bmatrix} 1 & 0 & 3 \\ 2 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$ Hence find A^{-1} and A^4 . (16)

Or

(b) Reduce the Quadratic form $x_1^2 + 2x_2^2 + x_3^2 - 2x_1x_2 + 2x_2x_3$ to the canonical form through an orthogonal transformation and hence show that it is positive semi definite. Give also a non-zero set of values which will make the quadratic form zero. (16)

