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Question Paper Code: 31051

B.E/B.Tech. DEGREE EXAMINATION, MAY 2017

Fifth Semester

Computer Science and Engineering

01UMA521 – DISCRETE MATHEMATICS

(Common to Information Technology)

(Regulation 2013)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 2 = 20 Marks)

1. Construct the truth table for the compound proposition $(p \rightarrow q) \leftrightarrow (\neg p \rightarrow \neg q)$.
2. Give an indirect proof of the theorem "If $3n + 2$ is odd, then n is odd".
3. How many permutations of $\{a, b, c, d, e, f, g\}$ and with a ?
4. Find the recurrence relation satisfying the equation $y_n = A(3)^n + B(-4)^n$.
5. Define a complete graph.
6. Give an example of a graph which contains an Eulerian circuit that is also a Hamiltonian circuit.
7. Define a field in an algebraic system.
8. Show that every cyclic group is abelian.
9. When is a lattice said to be bounded?
10. What values of the Boolean variables x and y satisfy $xy = x + y$?

PART - B (5 x 16 = 80 Marks)

11. (a) (i) Show that $(p \rightarrow q) \wedge (r \rightarrow s), (q \rightarrow t) \wedge (s \rightarrow u), \neg(t \wedge u)$ and $(p \rightarrow r) \Rightarrow \neg p$. (8)
- (ii) Obtain PDNF of $(P \wedge Q) \vee (\neg P \wedge R) \vee (Q \wedge R)$. Also find PCNF. (8)

Or

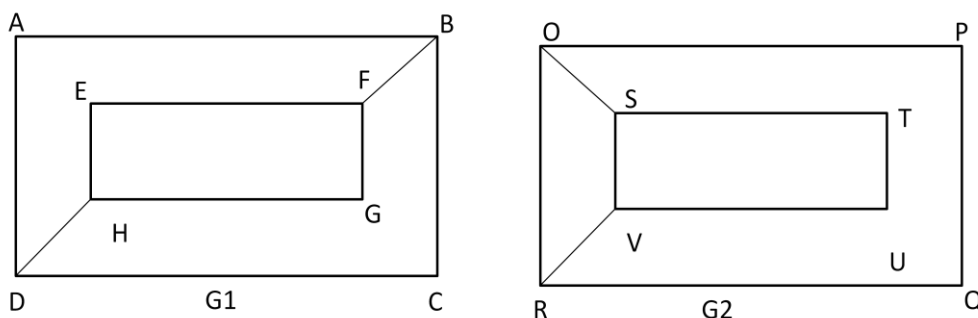
- (b) (i) Show that RVS follows logically from the premises $CVD, CVD \rightarrow 7H, 7H \rightarrow A \wedge 7B$ and $(A \wedge 7B) \rightarrow (RVS)$. (8)
- (ii) Prove that $\sqrt{2}$ is irrational by giving a proof of contradiction. (8)
12. (a) (i) Solve the recurrence relation $a_n = -3a_{n-1} - 3a_{n-2} - a_{n-3}$ with $a_0 = 5, a_1 = -9$ and $a_2 = 15$. (8)
- (ii) A man hiked for 10 hours and covered a total distance of 45 km. It is known that he hiked 6 km in the first hour and only 3 km in the last hour. Show that he must have hiked at least 9 km within a certain period of 2 consecutive hours. (8)

Or

- (b) (i) Solve the recurrence relation $a_n = 2a_{n-1} + 2^n, a_0 = 2$. (8)
- (ii) Prove the principle of inclusion – exclusion using mathematical induction. (8)
13. (a) (i) Describe a discrete structure based on a graph that can be used to model airline routes and their flight times. (8)
- (ii) Define an Euler path and show that if a graph G has more than two vertices of odd degree, then there can be no Euler path in G. (8)

Or

- (b) (i) If all the vertices of an undirected graph are each of degree k , show that the number of edges of the graph is a multiple of k . (8)
- (ii) Determine whether the graphs are isomorphic or not. (8)



14. (a) (i) State and prove Lagrange's theorem. (8)
- (ii) Show that the intersection of two normal sub groups of a group G is also a normal subgroup of G . (8)

Or

(b) (i) $(A,*)$ be a monoid such that for every x in A , $x * x = e$ where e is the identity element. Show that $(A,*)$ is an abelian group. (8)

(ii) State and prove the fundamental theorem on homomorphism of groups. (8)

15. (a) Show that the De Morgan's laws hold in a Boolean algebra. That is, show that for all x and y , $\overline{(x \vee y)} = \bar{x} \wedge \bar{y}$ and $\overline{(x \wedge y)} = \bar{x} \vee \bar{y}$. (16)

Or

(b) (i) Prove that the lattice of normal subgroups of a group G (with set inclusion) is a modular lattice. (8)

(ii) Show that a complemented, distributive lattice is a Boolean algebra. (8)

