

Reg. No. :

--	--	--	--	--	--	--	--	--	--	--

Question Paper Code: 31254

B.E. / B.Tech. DEGREE EXAMINATION, MAY 2017

Fifth Semester

Computer Science and Engineering

01UCS504 – THEORY OF COMPUTATION

(Regulation 2013)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 2 = 20 Marks)

1. Prove that “If p is a prime number bigger than 2, then p is odd”.
2. Define NFA with ϵ transition.
3. Define Regular expression. Give an example.
4. List the algorithms of minimizing the DFA.
5. Construct a CFG for the language $L = \{an, bn\} \ n \geq 1$.
6. Define Pushdown Automata.
7. Explain acceptance of PDA with empty stack.
8. Draw the transition diagram of a Turing Machine that can accept the language denoted by regular expression 11^* .
9. State some of NP-complete problems.
10. Define reducibility.

PART - B (5 x 16 = 80 Marks)

11. (a) (i) Prove by mathematical induction that for every integer $n \geq 0$ the number $4^{2n+1} + 3^{n+2}$ is multiple of 13. (6)
(ii) Show that a language L is accepted by some DFA if and only if L is accepted by some NFA. (10)

Or

- (b) The NFA with states $\{1, 2, 3, 4, 5\}$ and input alphabet $\{a, b\}$ has the following transition table. (i) Calculate $\delta(1, ab)$ (ii) Calculate $\delta(1, abab)$. (16)

	a	b
1	$\{1, 2\}$	$\{1\}$
2	$\{3\}$	$\{3\}$
3	$\{4\}$	$\{4\}$
4	$\{5\}$	Φ
5	Φ	$\{5\}$

12. (a) Let r be a regular expression. Then prove that there exists a NFA with ϵ transition that accept $L(r)$. (16)

Or

- (b) Construct a DFA equivalent to the following regular expression 01^*+1 . (16)
13. (a) Convert to Greibach Normal Form from the grammar $G=(\{A1, A2, A3\}, \{a, b\}, P, A1)$ where P consists of the following $A1 \rightarrow A2 A3$; $A2 \rightarrow A3 A1 | b$; $A3 \rightarrow A1 A2 | a$. (16)

Or

- (b) Find a Grammar in CNF equivalent to $S \rightarrow aAbB$, $A \rightarrow aA | a$, $B \rightarrow bB | b$. (16)
14. (a) Suppose L_1 is the context-free language generated by productions $\{B \rightarrow AB | \epsilon, A \rightarrow 011|1\}$ and L_2 is the context free language generated by the productions $\{C \rightarrow DC | \epsilon, D \rightarrow 01\}$. Construct the grammar generating language L_1L_2 . (16)

Or

- (b) Explain how the multiple tracks in a Turing Machine can be used for testing given positive integer is a prime or not. (16)
15. (a) Show that halting problem of Turing Machine is undecidable. (16)

Or

- (b) Define Computational Complexity? Explain whether the class of Problems that can be solved in polynomial time is equivalent to the class of non-deterministic polynomial problems i.e whether $P=NP$. (16)