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Question Paper Code: 54022

B.E. / B.Tech. DEGREE EXAMINATION, APRIL 2019

Fourth Semester

Civil Engineering

15UMA422 - NUMERICAL METHODS

(Common to EEE, EIE and Chemical Engineering)

(Regulation 2015)

Duration: Three hours

Maximum: 100 Marks

Answer ALL Questions

PART A - (10 x 1 = 10 Marks)

1. The sufficient condition for the convergence of iteration method is CO1- R
(a) $|f(x)f''(x)| > [f'(x)]^2$ (b) $|\phi'(x)| > 1$
(c) $|f(x)f''(x)| < [f'(x)]^2$ (d) $|\phi'(x)| < 1$
2. The condition for convergence of Gauss Jacobi method for solving a CO1- R
system of simultaneous algebraic equation is
(a) $|A| = 0$ (b) Orthogonal matrix
(c) $|A| \neq 0$ (d) Diagonally dominant system
3. Newton's forward interpolation formula is mainly applied to find the CO2- R
value of y using a given value of x only when 'x' falls
(a) At the beginning of the table (b) At the middle of the table
(c) At the end of the table (d) Far beyond the given upper value of 'x'
4. If only two pair values (x_0, y_0) and (x_1, y_1) are given then the CO2- R
Newton's forward formula reduces to
(a) Linear interpolation formula (b) Non-linear interpolation formula
(c) Parabolic interpolation formula (d) Exponential polynomial
5. The process of numerical integration of a function of a single variable CO3- R
is called
(a) Trapezoidal rule (b) Simpson's rule (c) Cubature (d) Quadrature

6. The order of error in the Trapezoidal rule is CO3- R
 (a) $O(h^4)$ (b) $O(h^3)$ (c) $O(h^5)$ (d) $O(h^2)$
7. Runge-Kutta method of first order is same as CO4- R
 (a) Euler's method (b) Modified Euler's method
 (c) Taylor series method (d) Milne's method
8. The number of prior values required to predict the next value in Milne's method is CO4- R
 (a) 4 (b) 6 (c) 5 (d) 2
9. The equation $u_{xx} + u_{yy} = 0$ is of CO5- R
 (a) Elliptic type (b) Parabolic type
 (c) Hyperbolic type (d) Non homogeneous type
10. The interval in which the implicit formula (Crank- Nicholson) provides stable solution is CO5- R
 (a) $0 < \lambda \leq 1$ (b) $0 < \lambda \leq 2$ (c) $1 < \lambda \leq 2$ (d) $0 < \lambda \leq \frac{1}{2}$

PART – B (5 x 2= 10 Marks)

11. Find the interval for a positive root of the polynomial $x^3 - 2x + 5 = 0$. CO1- App
12. Find $y(1)$ using Lagrange's interpolation formula from the given data: CO2- App
 $x : 0 \quad 1 \quad 3$
 $y : 5 \quad 6 \quad 50$
13. Find $\int_0^1 \frac{dx}{1+x}$ using two-point Gaussian quadrature formula. CO3- App
14. Find $y(1.1)$ if $y' = x + y$, $y(1) = 0$ using Taylor's series method of second order. CO4- App
15. State Crank – Nicholson difference scheme to solve a parabolic equation. CO5- R

PART – C (5 x 16= 80Marks)

16. (a) (i) Solve the following system of equations by Gauss elimination method, $2x + 3y - z = 5$, $4x + 4y - 3z = 3$, $2x - 3y + 2z = 2$ CO1- App (8)
- (ii) Solve the system of equations $28x + 4y - z = 32$, $x + 3y + 10z = 24$, $2x + 17y + 4z = 35$ by Gauss-Seidel Method. CO1- App (8)

Or

(b) (i) Find the positive root of $f(x) = 2x^3 - 3x - 6 = 0$, by N-R method. CO1- App (8)

(ii) Determine the largest eigen value and the corresponding eigen vector of CO1- App (8)

$$A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ -10 & -1 & 2 \end{bmatrix} \text{ by power method.}$$

17. (a) (i) Find y at $x = 43$, by using Newton's forward interpolation formula from the following data, CO2- App (8)

| | | | | | | |
|---|-----|-----|-----|-----|-----|-----|
| x | 40 | 50 | 60 | 70 | 80 | 90 |
| y | 184 | 204 | 226 | 250 | 276 | 304 |

(ii) The population of a town in the census is as given in the data. CO2- App (8)
Estimate the population in the year 1996 using Newton's backward interpolation.

| | | | | | |
|-----------------------|------|------|------|------|------|
| Year (x) | 1961 | 1971 | 1981 | 1991 | 2001 |
| Population (in 000's) | 46 | 66 | 81 | 93 | 101 |

Or

(b) (i) Using Newton's divided difference formula, find values of $f(2)$ from the following data. CO2- App (8)

| | | | | | | |
|------|----|-----|-----|-----|------|------|
| x | 4 | 5 | 7 | 10 | 11 | 13 |
| f(x) | 48 | 100 | 294 | 900 | 1210 | 2028 |

(ii) Find $f(27)$ by using Lagrange's formula for the data given below. CO2- App (8)

| | | | | |
|------|------|------|------|------|
| x | 14 | 17 | 31 | 35 |
| f(x) | 68.7 | 64.0 | 44.0 | 39.1 |

18. (a) (i) Find y' and y'' at $x = 1.5$ from the following table, CO3- Ana (8)

| | | | | | | |
|---|-------|-----|--------|------|--------|-----|
| x | 1.5 | 2.0 | 2.5 | 3.0 | 3.5 | 4.0 |
| y | 3.375 | 7.0 | 13.625 | 24.0 | 38.875 | 59 |

- (ii) Find $\int_{1.6}^{2.8} f(x) dx$ by Simpsons $(1/3)^{rd}$ rule from the following table. CO3- Ana (8)

| | | | | | | | |
|------|------|------|------|------|-------|-------|-------|
| x | 1.6 | 1.8 | 2.0 | 2.2 | 2.4 | 2.6 | 2.8 |
| f(x) | 4.95 | 6.05 | 7.39 | 9.02 | 11.02 | 13.46 | 16.44 |

Or

- (b) Evaluate $\int_0^1 \int_0^1 e^{x+y} dx dy$ using the Trapezoidal and Simpson's rules with $h = k = 0.5$ CO3- Ana (16)

19. (a) Solve $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ given $y(0) = 1$ at $x = 0.2$ and $x = 0.3$ using Runge – Kutta method of 4th order. CO4- App (16)

Or

- (b) (i) Find $y(0.2)$ correct to 3 decimals given $\frac{dy}{dx} = 1 - 2xy$, $y(0) = 0$ by using Taylor Series Method. CO4- App (8)
- (ii) Using Milne's method find $y(2)$ given $y' = \frac{1}{2}(x + y)$ given $y(0) = 2$, $y(0.5) = 2.636$, $y(1) = 3.595$ and $y(1.5) = 4.968$. CO4- App (8)

20. (a) Solve $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$, subject to CO5- App (16)

(i) $u(0,y) = 0, 0 \leq y \leq 4$

(ii) $u(4,y) = 12 + y, 0 \leq y \leq 4$

(iii) $u(x,0) = 3x, 0 \leq x \leq 4$

(iv) $u(x,4) = x^2, 0 \leq x \leq 4$ by dividing the square into 16 square meshes of side 1.

Or

- (b) Using Explicit scheme solve the wave equation $u_{tt} = u_{xx}$, $0 < x < 1, t > 0$, given $u(x, 0) = u_t(x,0) = u(0,t) = 0$ and $u(1,t) = 100 \sin(\pi t)$. Compute u for 4 times steps with $h = 0.25$. CO5- App (16)