

6. The necessary condition for the analyticity of a function is CO3- R

- (a) $u_x = v_y \& u_y = -v_x$ (b) $u_x = v_x \& u_y = -v_y$
 (c) $u_x = -v_y \& u_y = v_x$ (d) $u_x = v_y \& u_y = v_x$

7. The point $z = a$ is called a removable singularity of $f(z)$ if CO4- R

- (a) $\lim_{z \rightarrow a} f(z)$ exists (b) $\lim_{z \rightarrow -a} f(z)$ exists (c) $\lim_{z \rightarrow 0} f(z)$ exists (d) None of these

8. The poles of $\tan z$ are CO4- R

- (a) $z = n \frac{\pi}{2}$; n is odd (b) $z = \pm n \frac{\pi}{2}$; n is even
 (c) $z = \pm n \frac{\pi}{2}$; n is odd (d) $z = n \frac{\pi}{2}$; n is even

9. $L[e^{at}] =$ CO5- R

- (a) $\frac{1}{s+a}$ if $s+a > 0$ (b) $\frac{1}{s-a}$ if $s-a > 0$ (c) $\frac{a}{s-a}$ if $s-a > 0$ (d) $\frac{a}{s+a}$ if $s+a > 0$

10. The unit impulse function $\delta(t-a)$ is CO5- R

- (a) $\lim_{h \rightarrow 0} \frac{1}{h}$, $a \leq t \leq a+h$ (b) $\lim_{h \rightarrow 0} \frac{1}{h}$, $a \leq t < a+h$
 (c) $\lim_{h \rightarrow 0} \frac{1}{h}$, $a < t \leq a+h$ (d) $\lim_{h \rightarrow 0} \frac{1}{h}$, $a < t < a+h$

PART – B (5 x 2= 10 Marks)

11. Transform CO1- R

$(3x+2)^2 \frac{d^2y}{dx^2} + 3(3x+2) \frac{dy}{dx} - 36y = 0$ into differential equation with constant coefficient.

12. Find the value of λ , if CO2- R

$\vec{F} = (\lambda xy - z^3) \vec{i} + (\lambda - 2)x^2 \vec{j} + (1 - \lambda)xz^2 \vec{k}$ is irrotational.

13. State Cauchy-Riemann equations in Cartesian coordinates. CO3- R

14. Evaluate CO4- R

$$\int_C \frac{dz}{z+4} \text{ where } C \text{ is the circle } |z|=2.$$

15. Find $L[\cos at]$. CO5- R

PART – C (5 x 16= 80 Marks)

16. (a) (i) Solve $(D^2 - 4D - 5)y = e^{2x} + 3 \cos 4x.$ CO1- App (8)

(ii) Solve $[(1+x)^2 D^2 + (1+x)D + 1]y = \cos 2\log(1+x).$ CO1- App (8)

Or

(b) (i) Solve $(D^2 - 4D + 4)y = e^{2x}$ by the method of variation of parameters. CO1- App (8)

(ii) Solve $(x^2 D^2 - 7xD + 12)y = x^2.$ CO1- App (8)

17. (a) Verify Green's theorem for CO2- E (16)

$\int_C (3x^2 - 8y^2)dx + (4y - 6xy)dy,$ where C is the region bounded

by the lines $x = 0, y = 0, x + y = 1.$

Or

(b) Verify Gauss divergence theorem for CO2- E (16)

$\vec{F} = xz \vec{i} + 4xy \vec{j} - z^2 \vec{k}$ over the cube bounded by

$x = 0, x = 2, y = 0, y = 2, z = 0$ and $z = 2.$

18. (a) (i) Determine the analytic function CO3- Ana (8)

$f(z) = u + iv$ if

$v = e^{2x}(ycos2y + xsin2y).$

(ii) Find the bilinear transformation which maps the points CO3- Ana (8)
 $z = \infty, i, 0$ into $w = 0, i, \infty$ respectively.

Or

(b) Prove that the function $v = e^{-x}(x \cos y + y \sin y)$ is harmonic and CO3- Ana (16)
determine the corresponding analytic function $f(z).$

19. (a) (i) Using Cauchy's integral formula evaluate CO4- Ana (8)

$\int_C \frac{z^2}{(z-1)(z+3)} dz$ where C is the circle $|z-1|=2.$

(ii) Expand CO4- Ana (8)

$f(z) = \frac{z^2 - 1}{(z+2)(z+3)}$ as a Laurent series valid in the
region (i) $|z| < 2$ (ii) $|z| > 3.$

Or

(b) Evaluate CO4- E (16)

$$\int_{-\infty}^{\infty} \frac{x^2}{(x^2 + a^2)(x^2 + b^2)} dx, \quad a > 0, b > 0 \text{ by using Contour integration.}$$

20. (a) (i) Find the Laplace transform of CO5- App (8)

$$f(t) = \begin{cases} k, & 0 \leq t \leq a \\ -k, & a \leq t \leq 2a \end{cases};$$
$$f(t+2a) = f(t) \quad \forall t.$$

(ii) Find CO5- App (8)

$$L^{-1} \left[\frac{1}{(s+1)(s+3)} \right] \text{ using partial fraction method.}$$

Or

(b) (i) Find CO5- App (8)

$$L \left[\frac{\cos 2t - \cos 3t}{t} \right].$$

(ii) Solve by using Laplace transform technique, CO5- App (8)

$$y'' + 5y' + 6y = 2 \text{ given that } y(0) = 0 \text{ and } y'(0) = 0.$$